

CS660: Intro to Database Systems

Class 14: Query Processing with Relational Operations

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<https://bu-disc.github.io/CS660/>

Query Processing

Overview

Selections

Projections

Nested loop joins

Sort-merge and hash joins

General joins and aggregates

Query Processing

Overview

Readings: Chapter 12

Selections

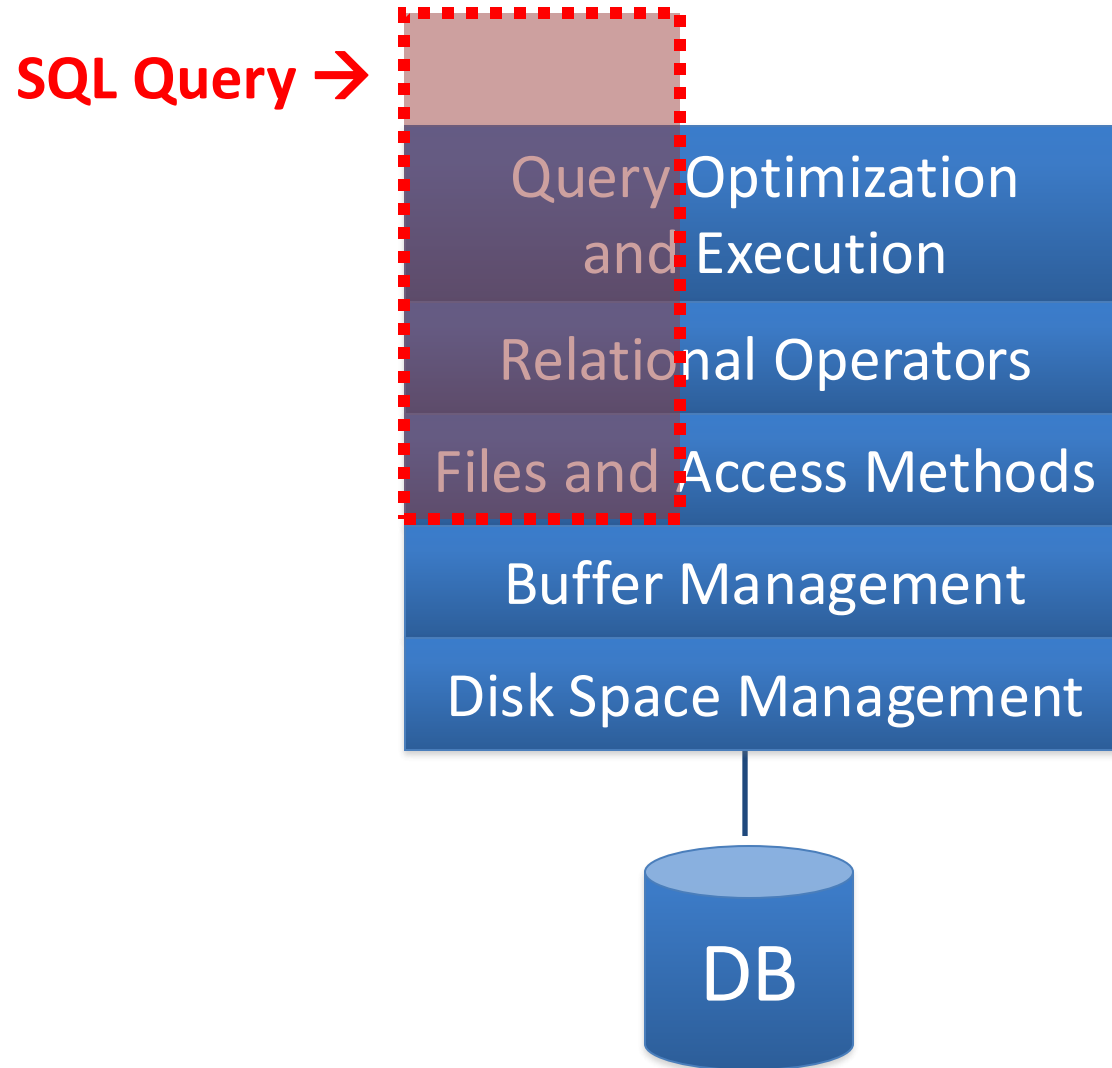
Projections

Nested loop joins

Sort-merge and hash joins

General joins and aggregates

DBMS Layer-Cake



SINGLE-TABLE QUERIES

Basic Single-Table Queries

```
SELECT [DISTINCT] <column expression list>  
FROM <single table>  
[WHERE <predicate>]  
[GROUP BY <column list>  
[HAVING <predicate>] ]  
[ORDER BY <column list>]
```

Basic Single-Table Queries

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FROM <single table>  
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[ORDER BY <column list>]
```

Simplest version is straightforward:

- Produce **all tuples** in the table that **satisfy the predicate**
- Output the **expressions** in the **SELECT** list
 - Expression can be a **column reference**, or an **arithmetic expression over column references**

Basic Single-Table Queries

```
SELECT S.name, S.gpa
FROM Students S
WHERE S.dept="CS"
[GROUP BY <column list>
[HAVING <predicate>] ]
[ORDER BY <column list>]
```

Simplest version is straightforward:

- Produce **all tuples** in the table that **satisfy the predicate**
- Output the **expressions** in the **SELECT** list
 - Expression can be a **column reference**, or an **arithmetic expression over column references**

SELECT DISTINCT

```
SELECT DISTINCT S.name, S.gpa
FROM Students S
WHERE S.dept="CS"
[GROUP BY <column list>
[HAVING <predicate>] ]
[ORDER BY <column list>]
```

The **DISTINCT** flag specifies removal of duplicates before output

ORDER BY

```
SELECT DISTINCT S.name, S.gpa, 2023-S.age AS YOB
FROM Students S
WHERE S.dept="CS"
[GROUP BY <column list>
[HAVING <predicate>] ]
ORDER BY S.gpa, S.name, YOB
```

ORDER BY clause specifies that output should be sorted

- Lexicographic ordering again!

Obviously must refer to **columns in the output (SELECT clause)**

- Note the **AS** clause for naming output columns!

ORDER BY

```
SELECT DISTINCT S.name, S.gpa
FROM Students S
WHERE S.dept="CS"
[GROUP BY <column list>
[HAVING <predicate>] ]
ORDER BY S.gpa DESC, S.name ASC
```

Ascending order by default, but can be overridden

- **DESC** flag for descending, **ASC** for ascending
- Can **mix and match**, lexicographically

AGGREGATES

```
SELECT [DISTINCT] AVERAGE(S.gpa)
FROM Students S
WHERE S.dept="CS"
[GROUP BY <column list>
[HAVING <predicate>] ]
[ORDER BY <column list>]
```

Before producing output, compute a **summary** (a.k.a. an **aggregate**) of some **arithmetic expression**

- Produces **1 row of output**
 - with one column in this case
- Other aggregates: **SUM, COUNT, MAX, MIN**

Note: can use **DISTINCT** inside the aggregate function (**what is the difference?**)

- SELECT **COUNT(DISTINCT S.name)** FROM Students S
- vs. SELECT **DISTINCT COUNT (S.name)** FROM Students S;



GROUP BY

```
SELECT [DISTINCT] AVERAGE(S.gpa), S.dept
FROM Students S
[WHERE <predicate>]
GROUP BY S.dept
[HAVING <predicate> ]
[ORDER BY <column list>]
```

Partition the table into **groups** that have the **same value on GROUP BY columns**

- Can group by a list of columns

Produce an **aggregate result per group**

- Cardinality of output = # of distinct group values

Note: can put grouping columns in SELECT list

- For aggregate queries, SELECT list can contain aggs and GROUP BY columns only!
- What would it mean if we said `SELECT S.name, AVERAGE(S.gpa)` above?



HAVING

```
SELECT [DISTINCT] AVERAGE(S.gpa), S.dept
FROM Students S
[WHERE <predicate>]
GROUP BY S.dept
HAVING COUNT(*)>5
[ORDER BY <column list>]
```

The **HAVING** predicate is applied **after grouping and aggregation**

- Hence can contain anything that could go in the **SELECT** list
- i.e. aggregates or **GROUP BY** columns

It is an **optional** clause

Putting it All Together

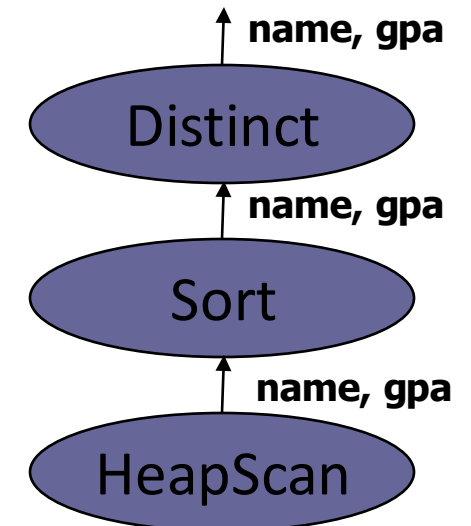
```
SELECT [DISTINCT] AVERAGE(S.gpa), S.dept
FROM Students S
WHERE S.age = 20
GROUP BY S.dept
HAVING COUNT(*)>5
ORDER BY S.dept;
```

Query Processing Overview

- The *query parser and optimizer* translates SQL to a special internal “language”
 - Query Plans
- The *query executor* is an *interpreter* for query plans
- Think of query plans as “box-and-arrow” *dataflow* diagrams
 - Each **box** implements a *relational operator*
 - **Edges** represent a **flow of tuples** (columns as specified)
 - For **single-table queries**, these diagrams are **straight-line graphs**

```
SELECT DISTINCT name, gpa  
FROM Students
```

Query Parsing & Optimization



Query processing

Some database operations are **EXPENSIVE**

Can greatly improve performance by being ‘smart’

- e.g., can speed up 1,000,000x over naïve approach

Main weapons are:

1. Clever (**fast**) implementation techniques for operators
2. exploiting ‘**equivalencies**’ of relational operators
3. using **statistics** and cost models to choose among these

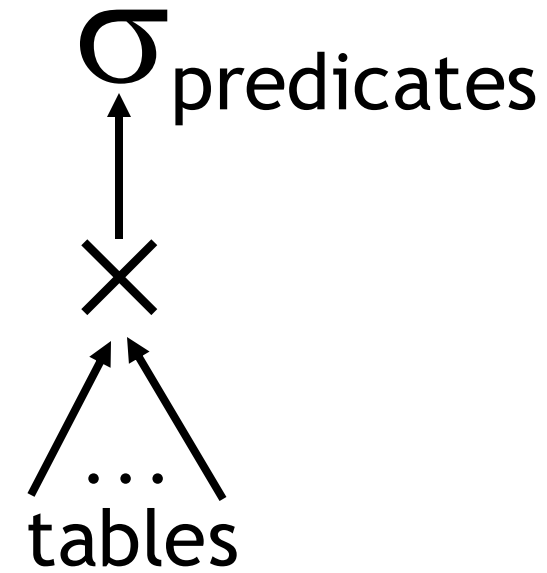
A Really Bad Query Optimizer

For each Select-From-Where query block

- Create a plan that:
 - Forms the Cartesian product of the FROM clause
 - Applies the WHERE clause
 - Incredibly inefficient
 - Huge intermediate results!

Then, as needed:

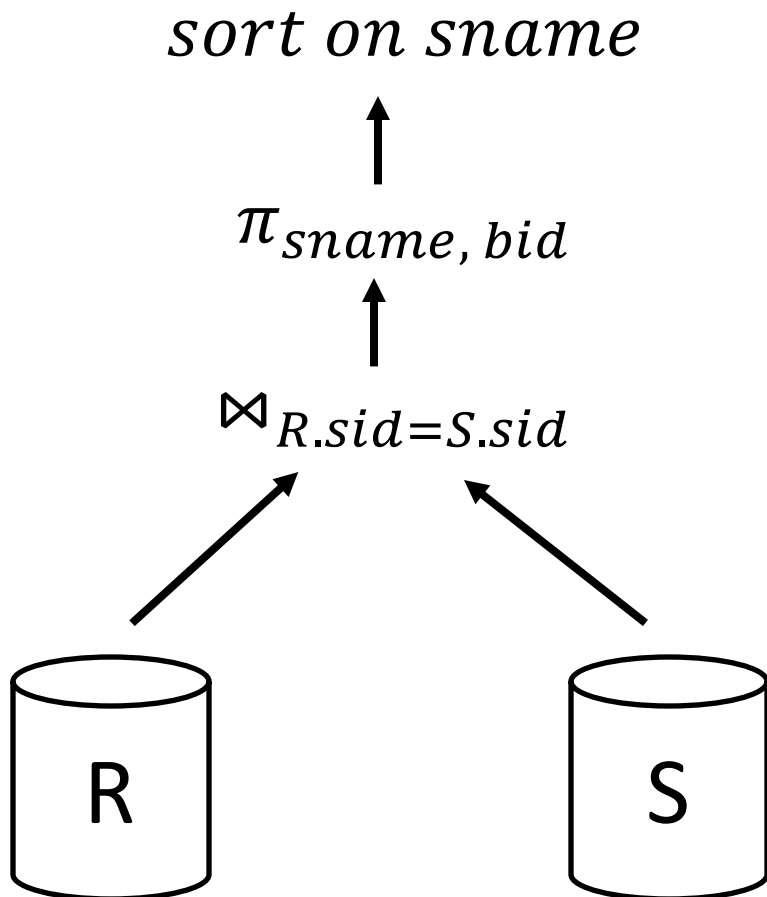
- Apply the GROUP BY clause
- Apply the HAVING clause
- Apply any projections and output expressions
- Apply duplicate elimination and/or ORDER BY



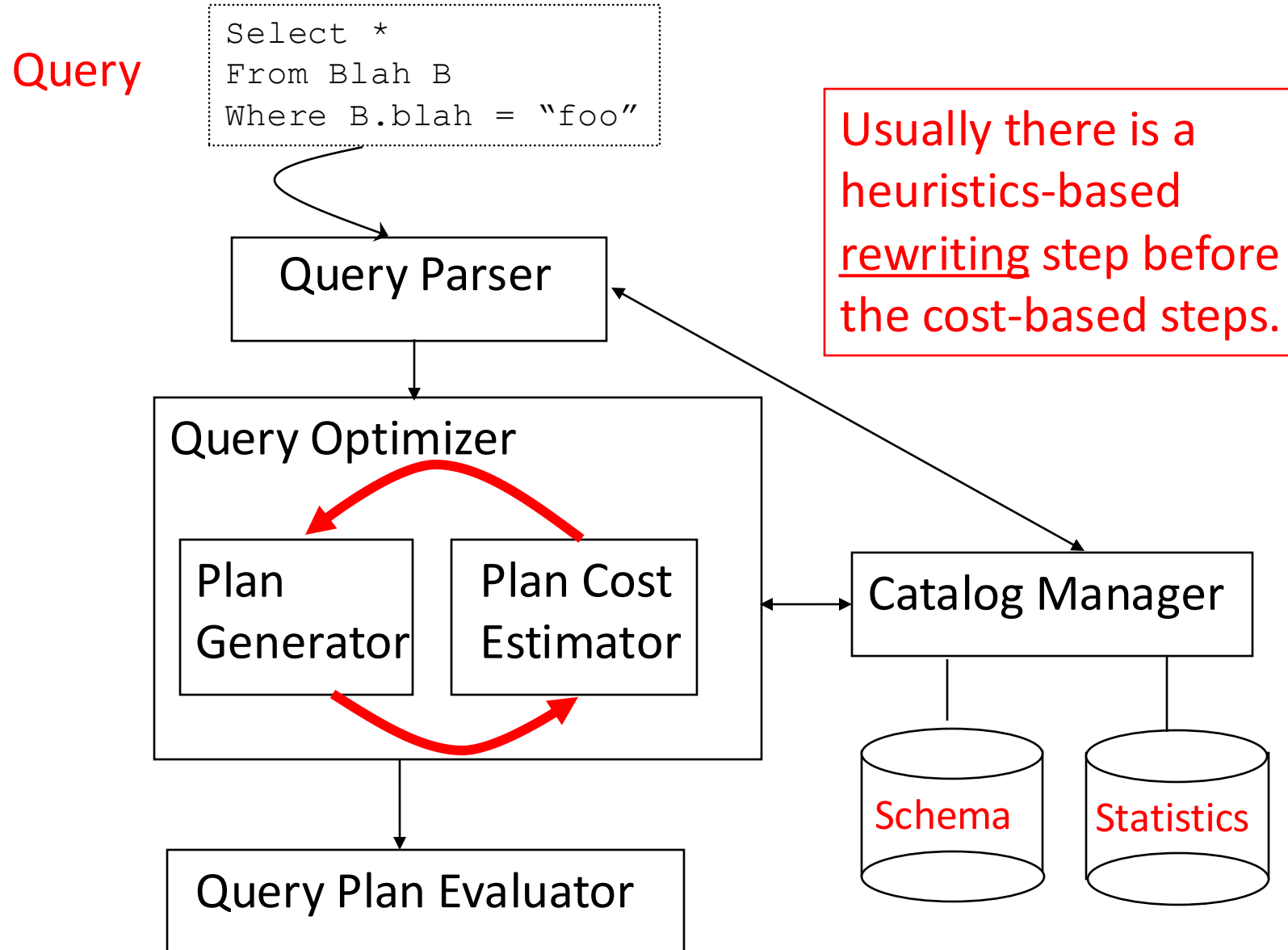
Correct BUT (very) slow!

A (multi-table) Query Plan

```
SELECT  sname, bid
FROM    R, S
WHERE   R.sid=S.sid
ORDER BY sname
```



Query execution



The Query Optimization Game

‘Optimizer’ is a bit of a misnomer

Goal: pick a ‘good’ (i.e., low expected cost) plan

- Involves choosing access methods, physical operators, operator orders, ...
- Notion of cost is based on an abstract ‘cost model’

Roadmap for this topic:

- First: basic operators
- Then: joins
- After that: optimizing multiple operators

Relational Operations

We will consider how to implement:

- Selection (σ) Selects a subset of rows from relation
- Projection (π) Deletes unwanted columns from relation
- Join (\bowtie) Allows us to combine two relations
- Set-difference ($-$) Tuples in relation 1, but not in relation 2
- Union (\cup) Tuples in relation 1 and in relation 2
- Aggregation (SUM, MIN, etc.) and GROUP BY

Today

Operators can be *composed* !

Next: *optimizing* queries by composing them

Common Techniques

Indexing

use an index to examine tuples satisfying a specific condition

Iteration

examine all tuples one after the other

Partitioning (e.g., sorting or hashing)

decompose a problem into a less expensive collection of operations on partitions

Schema for Examples

S: $N=500$, $p_S=80$, $t_S=50b$

R: $M=1000$, $p_R=100$, $t_S=40b$

Sailors (*sid*: integer, *sname*: string, *rating*: integer, *age*: real)

Reserves (*sid*: integer, *bid*: integer, *day*: dates, *rname*: string)

Similar to old schema; *rname* added for variations.

Sailors:

- Each tuple is 50 bytes long, 80 tuples per page, 500 pages
- $N=500$, $p_S=80$, $t_S=50$

Reserves:

- Each tuple is 40 bytes long, 100 tuples per page, 1000 pages
- $M=1000$, $p_R=100$, $t_S=40$

Query Processing

Overview

Selections

Readings: Chapters 14.1-14.2

Projections

Nested loop joins

Sort-merge and hash joins

General joins and aggregates

Simple Selections

```
SELECT *  
FROM Reserves R  
WHERE R.rname < 'C%'
```

Of the form: $\sigma_{R.attr \text{ op } value}(R)$

Question: how best to perform? Depends on:

- available indexes/access paths
- expected size of the result (# of tuples and/or # of pages)

Size of result approximated as

*size of R * reduction factor*

- “reduction factor” is usually called selectivity
- estimate of selectivity is based on statistics

Alternatives for Simple Selections

R: M=1000, $p_R=100$, ts=40b

With no index, unsorted:

- Must essentially scan the whole relation
- cost is M (#pages in R); for “reserves” = 1000 I/Os

With no index, sorted:

- cost of binary search + number of pages containing results.
- For reserves = $\log_2(1000) = 10$ I/Os + $\lceil \text{selectivity} * \# \text{pages} \rceil$

With an index on selection attribute:

1. Use index to find qualifying data entries,
 2. then retrieve corresponding data records
- Note: Hash index useful only for equality selections

Simple Selections – Explained

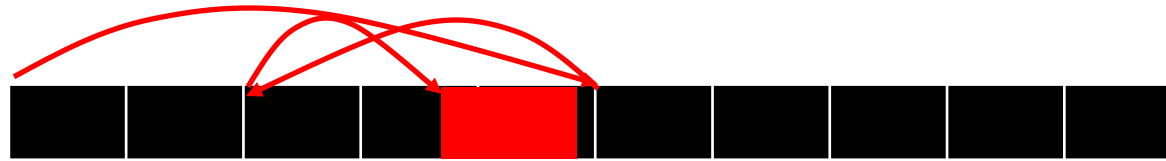
R: M=1000, p_R=100, ts=40b

1) no index, unsorted



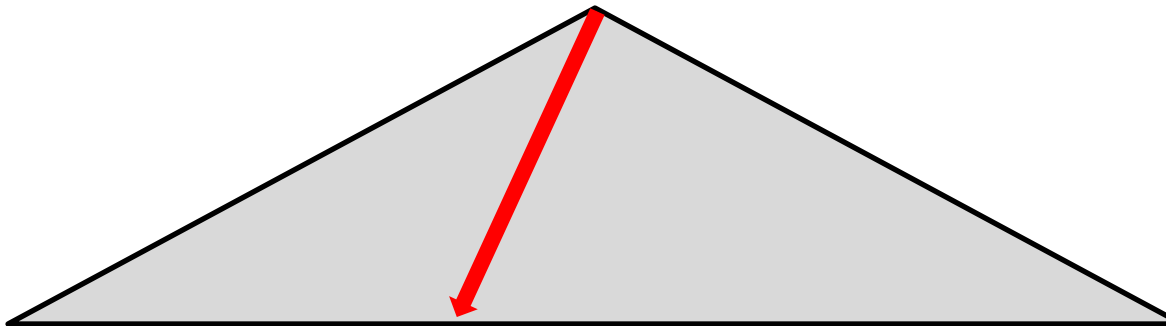
scan everything
cost=1000 I/O

2) no index, sorted



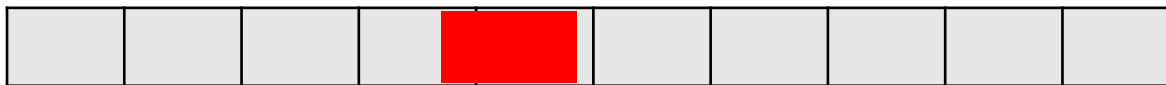
binary search: $\log_2 M$
qualifying pages: $\lceil f \cdot M \rceil$
selectivity

3) index



index search: $\log_B M$

data entries:



data records:



what is the cost to access
the qualifying pages?



Using an Index for Selections

Cost \sim #qualifying tuples, clustering

– Cost factors:

- find qualifying data entries (typically small)
- retrieve records (could be large w/o clustering)

– Our example, “reserves” relation:

if 10% of tuples qualify (100 pages, 10000 tuples)

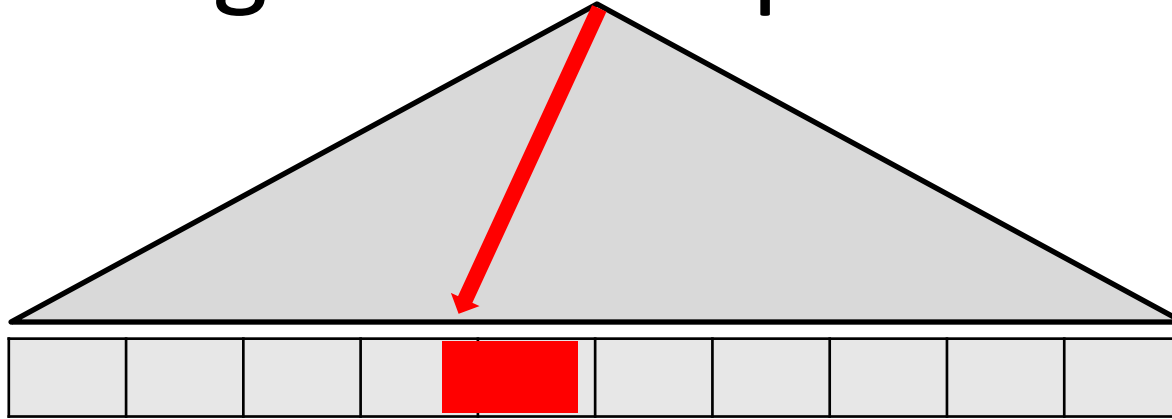
- *clustered* index \rightarrow a bit more than 100 I/Os
- *unclustered* \rightarrow could be up to 10000 I/Os!

Selections using Index– Explained

R: $M=1000$, $p_R=100$, $ts=40b$

A) clustered

data entries:



data records:



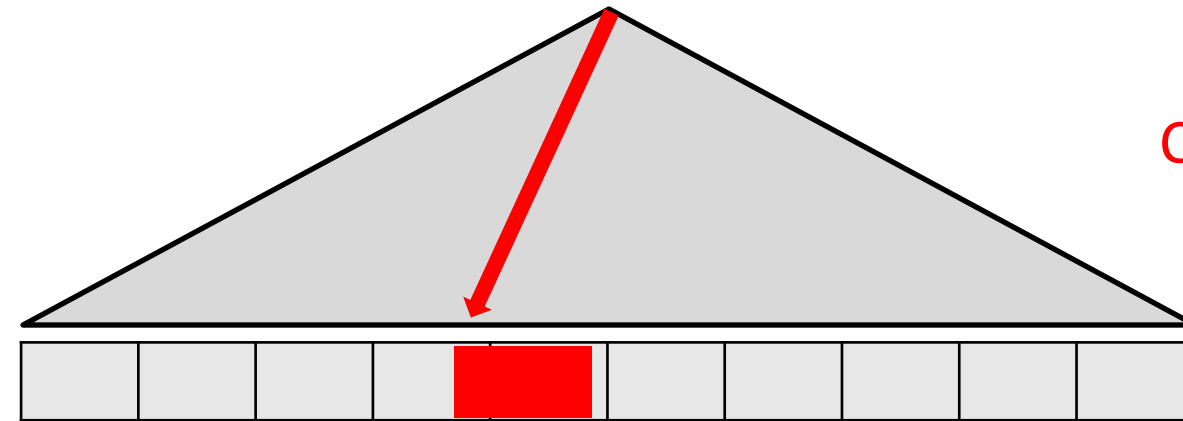
index search: $\log_B M$

$$[f \cdot M] = 10\% \cdot 1000 = 100$$

Can we do better? 

B) unclustered

data entries:



data records:



index search: $\log_B M$

$$[f \cdot M \cdot p_R] = 10\% \cdot 1000 \cdot 100 = 10000$$

Selections using Index -- Refinement

R: $M=1000$, $p_R=100$, $ts=40b$

*Important refinement
(for unclustered):*

A) clustered

data entries:



data records:



1. Find qualifying data entries

2. Sort the rid's of the data records to be retrieved

3. Fetch rid's in order

Each data page is accessed once

B) unclustered

data entries:



data records:



No need for clustered!

General Selection Conditions

- *(day < 8/9/94 AND rname = 'Paul') OR bid = 5 OR sid = 3*

First converted to conjunctive normal form (CNF)

- *(day < 8/9/94 OR bid = 5 OR sid = 3) AND (rname = 'Paul' OR bid = 5 OR sid = 3)*

We assume no ORs (conjunction of *<attr op value>*)

A **B-tree** index matches (a conjunction of) terms that involve only attributes in a *prefix* of the search key

- Index on *<a, b, c>* matches *a = 5 AND b = 3*, but not *b = 3*

Hash indexes must have all attributes in search key

Hash indexes support only...?



Selections – 1st approach

1. Find the *cheapest access path*
2. Retrieve tuples using it
3. Apply the terms that don't **match** the index (if any):
 - *Cheapest access path*
An index or file scan with the fewest estimated page I/Os
 - **Terms that match** this index reduce the # of tuples *retrieved*
 - **Other terms** are used to discard some retrieved tuples, but do not affect number of tuples/pages fetched

Cheapest Access Path - Example

Consider *day < 8/9/94 AND bid=5 AND sid=3*

A **B+ tree index on day** can be used;

- then, *bid=5* and *sid=3* must be checked for each retrieved tuple

Similarly, a hash index on $\langle bid, sid \rangle$ could be used;

- Then, *day < 8/9/94* must be checked

How about a B+tree on $\langle rname, day \rangle$?

How about a B+tree on $\langle day, rname \rangle$?

How about a Hash index on $\langle day, rname \rangle$?



Selections – 2nd approach: Intersecting RIDs

If we have 2 or more matching indexes (w/Alt. (2) or (3) for data entries):

1. Get **sets of rids** of data records using **each** matching index
2. Then **intersect** these **sets of rids**
3. Retrieve the records and apply any remaining terms

EXAMPLE: Consider ***day<8/9/94 AND bid=5 AND sid=3***

– With (i) a **B+ tree index on *day*** and (ii) an **index on *sid***:

1. a) Retrieve rids of records satisfying ***day<8/9/94*** using the first
b) Retrieve rids of records satisfying ***sid=3*** using the second
2. **Intersect**
3. Retrieve records and check ***bid=5***

Selections: summary

Simple selections

- On sorted or unsorted data, with or without index

General selections

- Expressed in conjunctive normal form (**expr1 AND expr2 AND ...**)
- Retrieve tuples and then filter them through other conditions
- Intersect RIDs of matching tuples for non-clustered indexes

Choices depend on selectivity of each access method

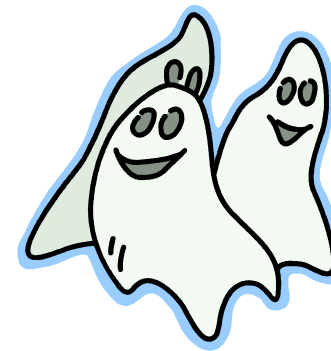
Break: The Halloween Problem



Story from the early days of System R.

While testing the optimizer on **10/31/76(?)**, the following update was run:

```
UPDATE payroll
SET salary = salary*1.1
WHERE salary < 25K;
```



AND IT STOPPED WHEN ALL HAD salary \geq 25K!

Can you guess why? (hint: it was an optimizer bug...)

Query Processing

Overview

Selections

Projections

Readings: Chapter 14.3

Nested loop joins

Sort-merge and hash joins

General joins and aggregates

The Projection Operation

Issue is removing **duplicates**

```
SELECT  DISTINCT
        R.sid, R.bid
FROM    Reserves R
```

Reserves (*sid*: integer, *bid*: integer, *day*: dates, *rname*: string)

R: M=1000, $p_R=100$, $ts=40b$

output tuple size: 10b

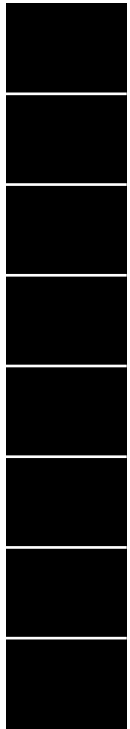
Basic approach is to use sorting

- 1. Scan R, extract only the needed attributes (why do this first?)
 - 2. Sort the resulting set
 - 3. Remove adjacent duplicates
- Cost: Reserves with size ratio 0.25 = 250 pages
 With 20 buffer pages can sort in 2 passes ($1 + \lceil \log_{19}(250/20) \rceil$), so:
 $1000 + 250 + 2 * 2 * 250 + 250 = 2500$ I/Os

Projection - Sorting (explained)

R: $M=1000$, $p_R=100$, $ts=40b$

output tuple size: 10b



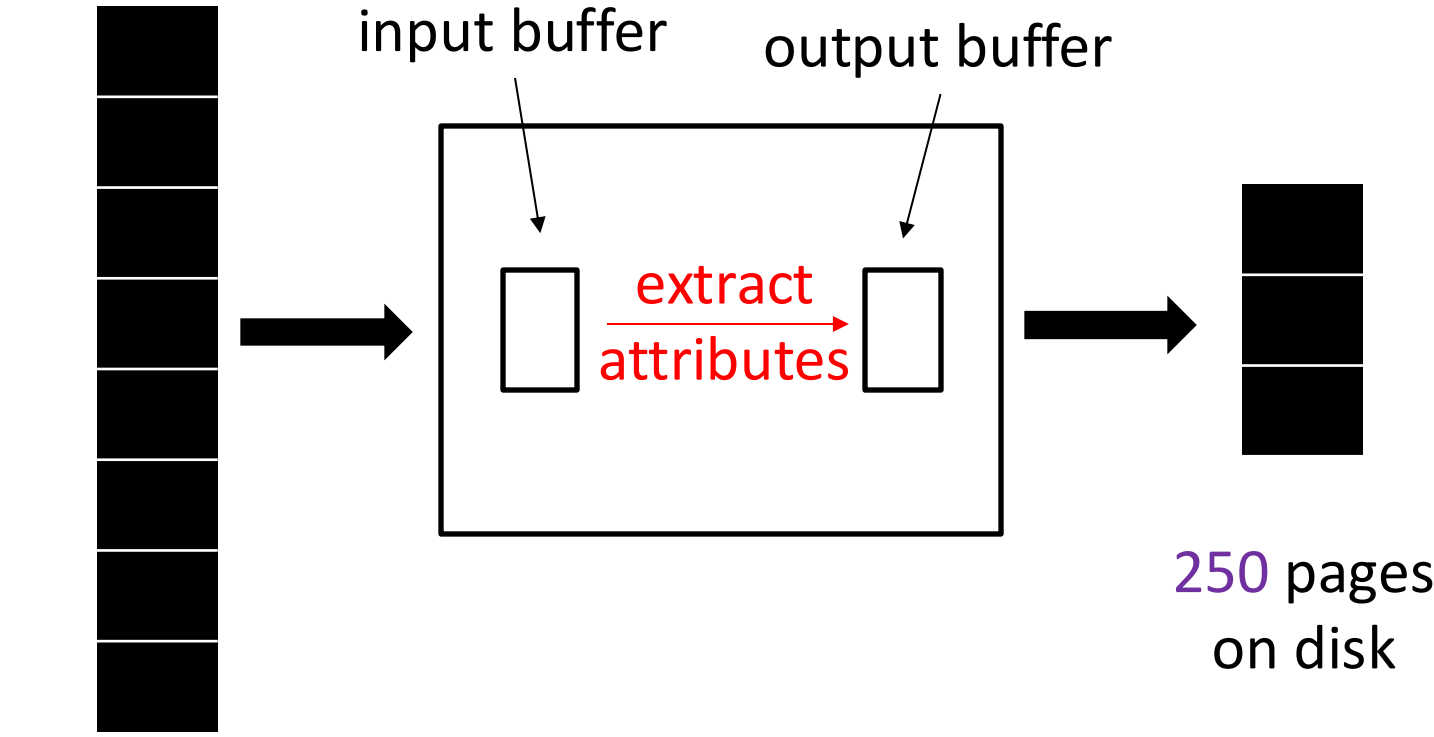
Remember the streaming paradigm?

1000 pages
on disk

Projection - Sorting (explained)

R: M=1000, p_R=100, ts=40b

output tuple size: 10b



1000 pages on disk

250 pages on disk

Note: if $B < \sqrt{M}$

$$1000 + 250 + \text{\#passes} * 2 * 250 + 250$$

Sorting to remove duplicates

B=20



Pass 0: $\lceil \frac{250}{20} \rceil = 13$ runs

Pass 1: final merge

Remove adjacent duplicates in final pass

Total cost:

$$1000 + 250 + 2 * 2 * 250 + 250 = 2500$$

Can we do better?



Projection: Yes, we can do better!

```
SELECT  DISTINCT
        R.sid, R.bid
FROM    Reserves R
```

Modify external sort algorithm (see chapter 13):

R: M=1000, $p_R=100$, ts=40b

output tuple size: 10b

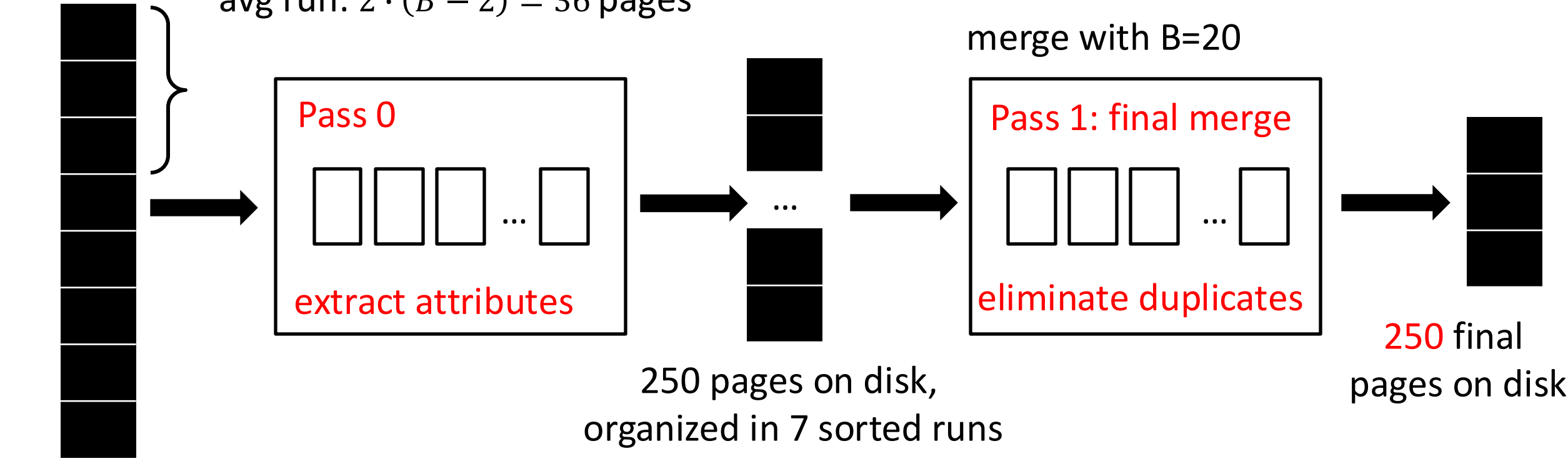
- Modify Pass 0 of external sort to eliminate unwanted fields
- Modify merging passes to eliminate duplicates
- Cost for above case:
read 1000 pages, write out 250 in runs of 40 pages,
merge runs = $1000 + 250 + 250 = 1500$

Projection - Sorting (explained)

R: M=1000, $p_R=100$, $ts=40b$

output tuple size: 10b

heapsort with $B=20$
 avg run: $2 \cdot (B - 2) = 36$ pages



1000 pages on disk

Pass 0: $\lceil \frac{250}{36} \rceil = 7$ runs

Total cost:
 $1000 + 250 + 250 = 1500$

Projection Based on *Hashing*

Partitioning phase:

- Read R using one input buffer
- For each tuple:
 - Discard unwanted fields
 - Apply hash function $h1$ to choose one of B-1 output buffers
- Result is B-1 partitions (of tuples with no unwanted fields)
 - 2 tuples from different partitions guaranteed to be distinct

Projection Based on *Hashing*

Duplicate elimination phase:

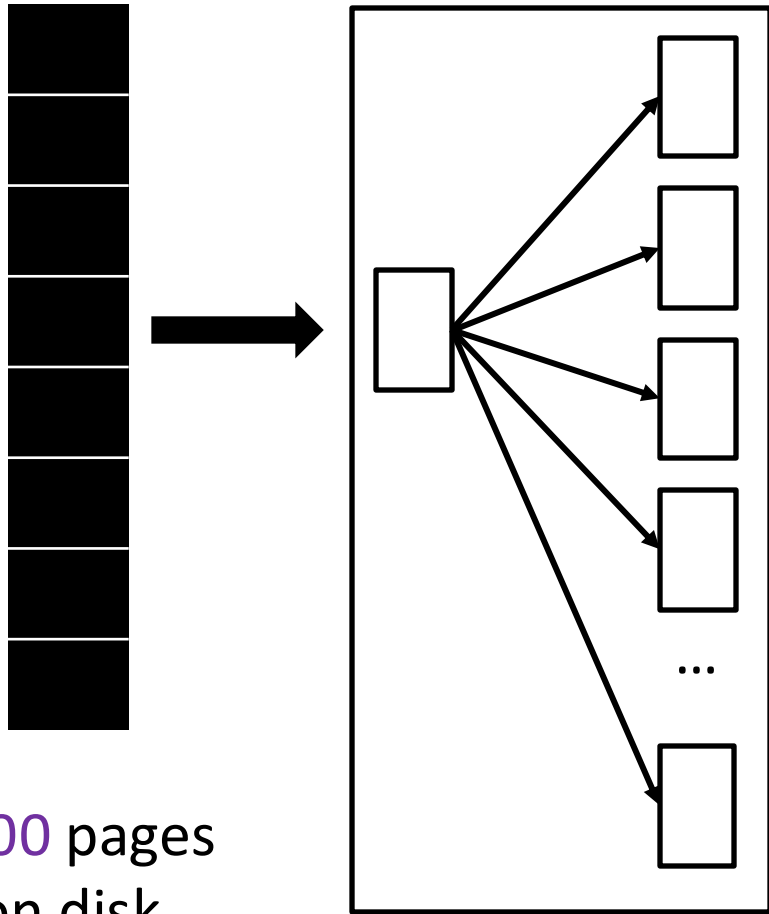
- For each partition
 - Read it and build an in-memory hash table
 - using hash function $h2$ ($\neq h1$) on all desired fields
 - while discarding duplicates
- If partition does not fit in memory
 - Apply hash-based projection algorithm recursively to this partition

Projection - Hashing (explained)

R: $M=1000$, $p_R=100$, $ts=40b$

output tuple size: 10b

hash partitioning with $B=20$

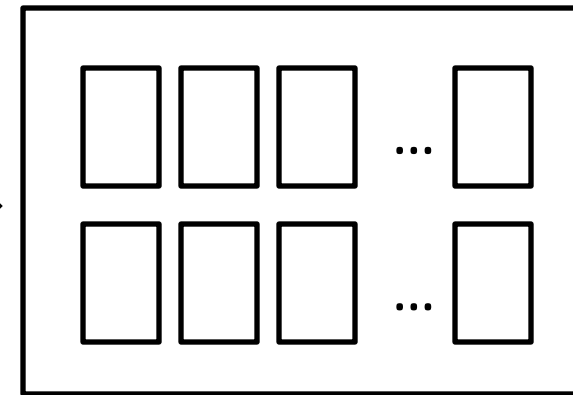


1000 pages on disk



250 pages on disk, in $B-1$ partitions
(any duplicates will be in the same partitions)

duplicate elimination with $B=20$



if all partitions fit in B pages, i.e., $B \geq \sqrt{M}$
(if not apply the hash partitioning algorithm recursively)



250 pages on disk

Total cost:

$$1000 + 250 + 250 = 1500$$

Discussion of Projection (1/2)

Sort-based approach is standard

- Better handling of **skew**, and result is **sorted**

If there are enough buffers, both have same I/O cost:

$$M + 2T$$

where:

- M is #pages in R,
- T is #pages of R with unneeded attributes removed

Although many systems don't use the specialized sort

Discussion of Projection (2/2)

If all wanted attributes are indexed

→ *index-only* scan

- Apply projection techniques to data entries (much smaller!)

If all wanted attributes are indexed as prefix of the search key

→ even better:

- Retrieve data entries in order (index-only scan)
- Discard unwanted fields
- Compare adjacent tuples to check for duplicates

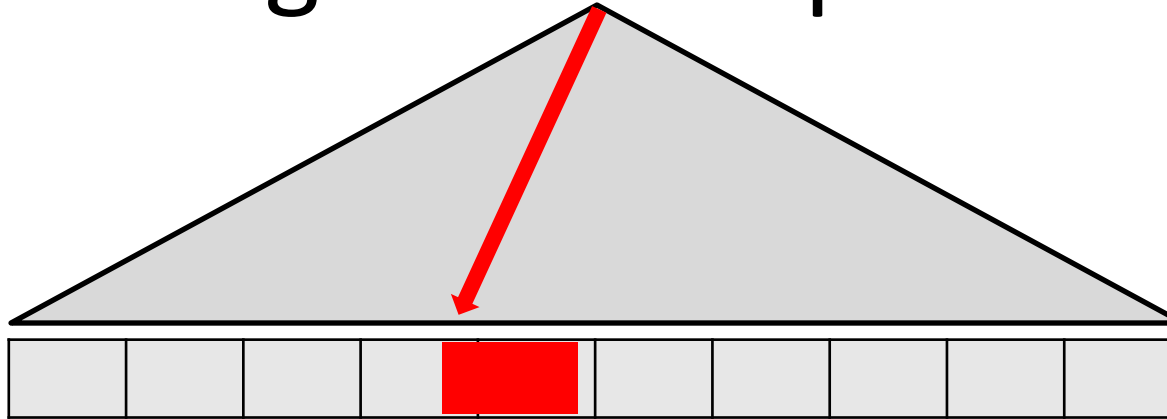
Projections using Index– Explained

R: M=1000, $p_R=100$, ts=40b

```
SELECT  DISTINCT
        R.sid, R.bid
FROM    Reserves R
```

A) indexed

data entries:



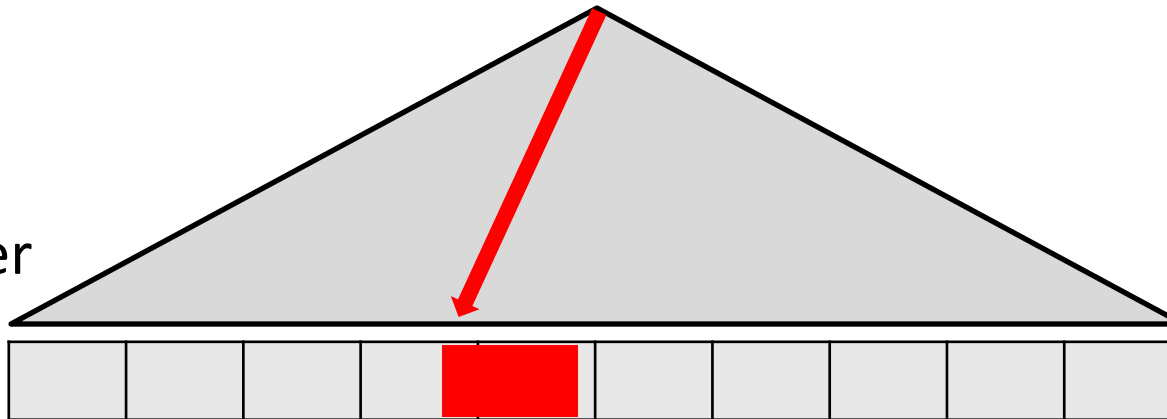
Index on <sid, day, bid>

no need to access the base data!

apply sort-based or hash-based projection only on the desired attributes

A) indexed in prefix order

data entries:



Index on <sid, bid, day >

retrieve entries sorted

discard unwanted fields & duplicates on the fly

Projections: summary

Projection based on *sorting*

Projection based on *hashing*

Can use *indexes* if they cover *relevant attributes*

Query Processing

Overview

Selections

Projections

Nested loop joins

Readings: Chapters 14.4-14.4.1

Sort-merge and hash joins

General joins and aggregates

Joins...

...are very common.

...can be very expensive (cross product in the worst case).

➔ Many approaches to reduce join cost!

Join techniques we will cover:

1. Nested-loops join
2. Index-nested loops join
3. Sort-merge join
4. Hash join

Equality Joins With One Join Column

```
SELECT *  
FROM Reserves R1, Sailors S1  
WHERE R1.sid=S1.sid
```

In algebra: $R \bowtie S$. Common! Must be carefully optimized. $R \times S$ is large; so, $R \times S$ followed by a selection is inefficient

Remember, join is associative and commutative

Assume:

- M pages in R, p_R tuples per page
- N pages in S, p_S tuples per page
- In our examples, R is Reserves and S is Sailors

We will consider more complex join conditions later

Cost metric : # of I/Os

We will ignore output costs

Simple Nested Loops Join

```
foreach tuple r in R do
  foreach tuple s in S do
    if ri == sj then add <r, s> to result
```

For each tuple in the *outer* relation R, we scan the entire *inner* relation S

How much does this Cost?

$$(p_R * M) * N + M = 100 * 1000 * 500 + 1000 \text{ I/Os}$$

– At 10ms/IO, Total: ???

What if smaller relation (S) was outer?

What assumptions are being made here?

Q: What is cost if one relation can fit entirely in memory?

Page-Oriented Nested Loops Join

```

foreach page  $b_R$  in R do
  foreach page  $b_S$  in S do
    foreach tuple  $r$  in  $b_R$  do
      foreach tuple  $s$  in  $b_S$  do
        if  $r_i == s_j$  then add  $\langle r, s \rangle$  to result
  
```

For each *page* of R

- get each *page* of S
- write out matching pairs of tuples $\langle r, s \rangle$, where r is in R-page and S is in S-page

What is the cost of this approach?

$$M * N + M = 1000 * 500 + 1000$$

- If smaller relation (S) is outer, cost = $500 * 1000 + 500$

Index Nested Loops Join

```
foreach tuple r in R do
  foreach tuple s in S where  $r_i == s_j$  do
    add <r, s> to result
```

If there is an index on the join column of one relation (say S), can make it the inner and exploit the index

– Cost: $M + (M * p_R) * \text{cost of finding matching S tuples}$

For each R tuple, cost of probing S index is about 1.2 for hash index, 2-4 for B+ tree. Cost of then finding S tuples (assuming Alt. (2) or (3) for data entries) depends on clustering

Clustered index: 1 I/O per page of matching S tuples

Unclustered: up to 1 I/O per matching S tuple

Examples of Index Nested Loops (1/2)

Hash-index (Alt. 2) on *sid* of Sailors (inner):

- Scan Reserves: 1000 page I/Os, $100 * 1000$ tuples
- For each Reserves tuple:
 - 1.2 I/Os to get data entry in index,
 - plus 1 I/O to get (the exactly one) matching Sailors tuple

Examples of Index Nested Loops (2/2)

Hash-index (Alt. 2) on *sid* of Reserves (inner):

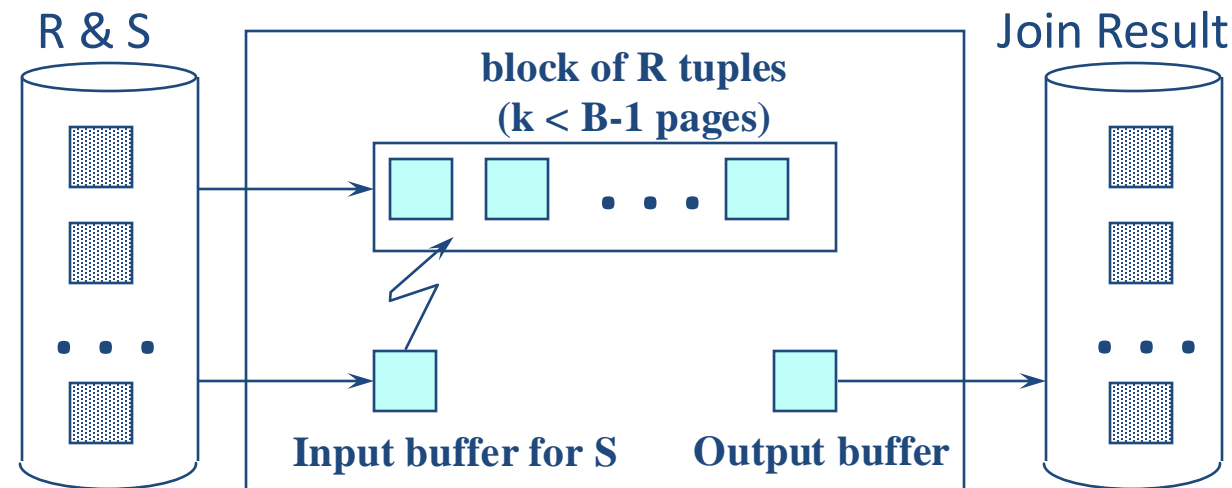
- Scan Sailors: 500 page I/Os, 80×500 tuples
- For each Sailors tuple:
 - 1.2 I/Os to find index page with data entries,
 - plus cost of retrieving matching Reserves tuples
 - **Assuming uniform distribution**, 2.5 reservations per sailor ($100,000 / 40,000$). Cost of retrieving them is 1 or 2.5 I/Os depending on whether the index is clustered

Block Nested Loops Join

Page-oriented NL doesn't exploit extra buffers

Alternative approach: Use one page as an input buffer for scanning the inner S, one page as the output buffer, and use all remaining pages to hold 'block' of outer R

For each matching tuple r in R-block, s in S-page, add $\langle r, s \rangle$ to result. Then read next R-block, scan S, etc



Examples of Block Nested Loops

Cost: Scan of outer + #outer blocks * scan of inner

– #outer blocks = $\lceil \# \text{ of pages of outer} / \text{blocksize} \rceil$

With Reserves (R) as outer, and 100 pages of R:

- Cost of scanning R is 1000 I/Os; a total of 10 *blocks*
- Per block of R, we scan Sailors (S); 10*500 I/Os

With 100-page block of Sailors as outer:

- Cost of scanning S is 500 I/Os; a total of 5 blocks
- Per block of S, we scan Reserves; 5*1000 I/Os

With sequential reads considered, analysis changes: may be best to divide buffers evenly between R and S

Nested loop joins: summary

Simple nested loops

- Optimized by page-oriented access

Index nested loops

- Costs depend on the type of index

Block nested loops

- Optimization of page nested loops which uses memory buffers

Query Processing

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Nested loop joins

Sort-merge and hash joins

Readings: Chapters 14.4.2-14.4.3

General joins and aggregates

Sort-Merge Join ($R \bowtie_{i=j} S$)

Sort R and S on the join column, then scan them to do a ‘merge’ (on join column), and output result tuples

Useful if

- one or both inputs are already sorted on join attribute(s)
- output is required to be sorted on join attributes(s)

‘Merge’ phase can require some back tracking if duplicate values appear in join column

R is scanned once; each S group is scanned once per matching R tuple. Note: Multiple scans of an S group will probably find needed pages in buffer

Example of Sort-Merge Join

<u>sid</u>	sname	rating	age
22	dustin	7	45.0
28	yuppy	9	35.0
31	lubber	8	55.5
44	guppy	5	35.0
58	rusty	10	35.0

<u>sid</u>	<u>bid</u>	<u>day</u>	rname
28	103	12/4/96	guppy
28	103	11/3/96	yuppy
31	101	10/10/96	dustin
31	102	10/12/96	lubber
31	101	10/11/96	lubber
58	103	11/12/96	dustin

Cost: Sort R + Sort S + (M+N)

- The cost of scanning, M+N, could be M*N (very unlikely!)

With 35, 100 or 300 buffer pages, both Reserves and Sailors can be sorted in 2 passes; total join cost: $2 * \#passes * (M+N) + (M+N) = 7500$

(BNL cost: 2500 to 15000 I/Os)

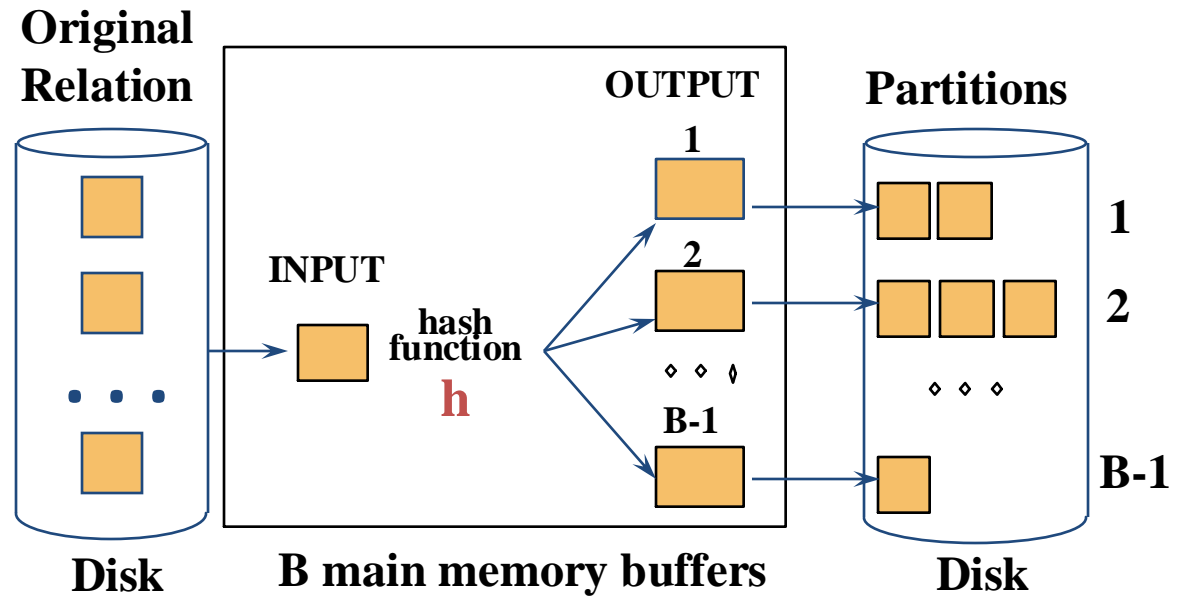
Refinement of Sort-Merge Join

We can combine the merging phases in the *sorting* of R and S with the merging required for the join

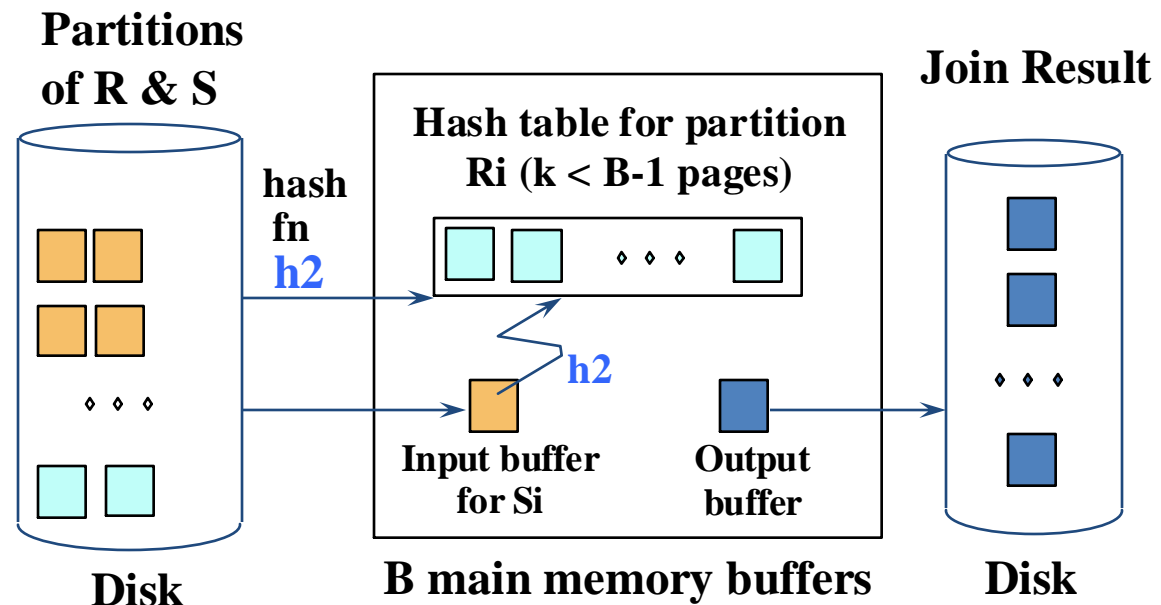
- Allocate 1 page per run of each relation, and ‘merge’ while checking the join condition
- With $B > \sqrt{L}$, where L is the size of the larger relation, using the sorting refinement that produces runs of length $2B$ in Pass 0, #runs of each relation is $< B/2$
- **Cost:** read+write each relation in Pass 0 + read each relation in (only) merging pass (+ writing of result tuples)
- In example, cost goes down from 7500 to 4500 I/Os

Hash-Join

Partition both relations using hash function h : R tuples in partition i will **only** match S tuples in partition i



Read in a partition of R , hash it using h_2 ($\neq h!$). Scan matching partition of S , probe hash table for matches



Observations on Hash-Join

First pass creates $B-1$ partitions, each of size $S_i = N/(B-1)$

Need each $S_i \leq B-2$ in order to fit in memory for 2nd pass

→ Need $N/(B-1) \leq B-2$

... or, roughly: $B > \sqrt{N}$ (we consider a fudge factor, f , so: $B > f\sqrt{N}$)

where N is size of smaller relation

More Observations on Hash-Join

Since we build an in-memory hash table to speed up the matching of tuples in the second phase, a little more memory is needed

If the hash function does not partition uniformly, one or more R partitions may not fit in memory. We can apply hash-join technique recursively to do the join of this R-partition with corresponding S-partition

Cost of Hash-Join

In partitioning phase, **read and write** both relations; $2(M+N)$

In matching phase, **read** both relations; $M+N$ I/Os

In our running example, this is a total of 4500 I/Os

Sort-Merge Join vs. Hash Join

Given a minimum amount of memory (*what is this, for each?*) both have a cost of $3(M+N)$ I/Os

Hash Join Pros:

- Superior if relation sizes differ greatly
- Shown to be highly parallelizable (*beyond scope of class*)

Sort-Merge Join Pros:

- Less sensitive to data skew
- Result is sorted (may help “upstream” operators)
- Goes faster if one or both inputs already sorted

Hash-Join

Let $B = 5$

Buckets:

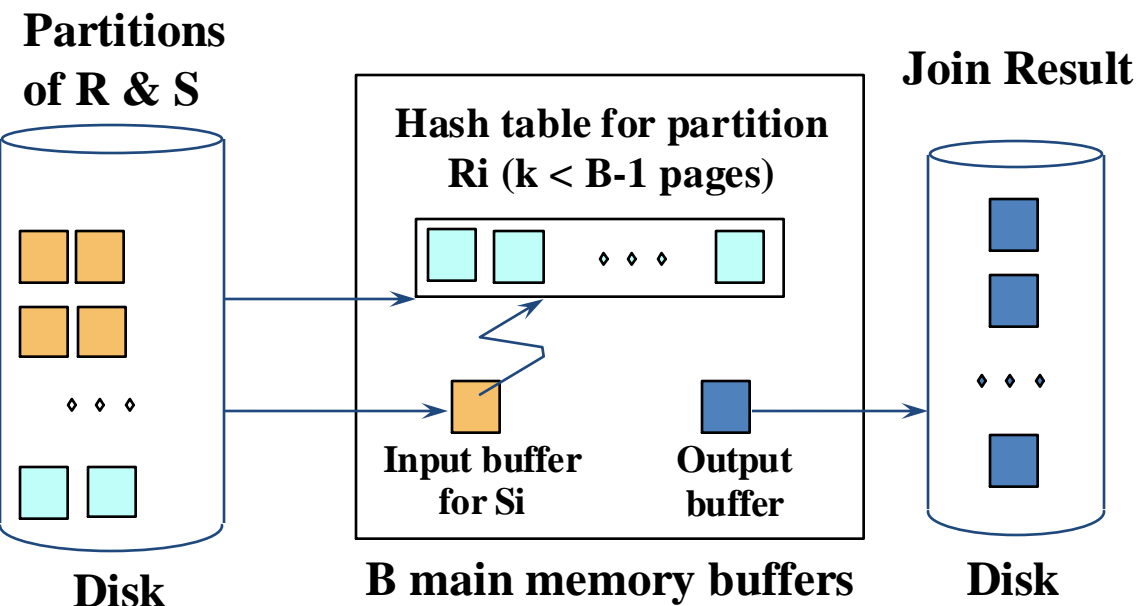
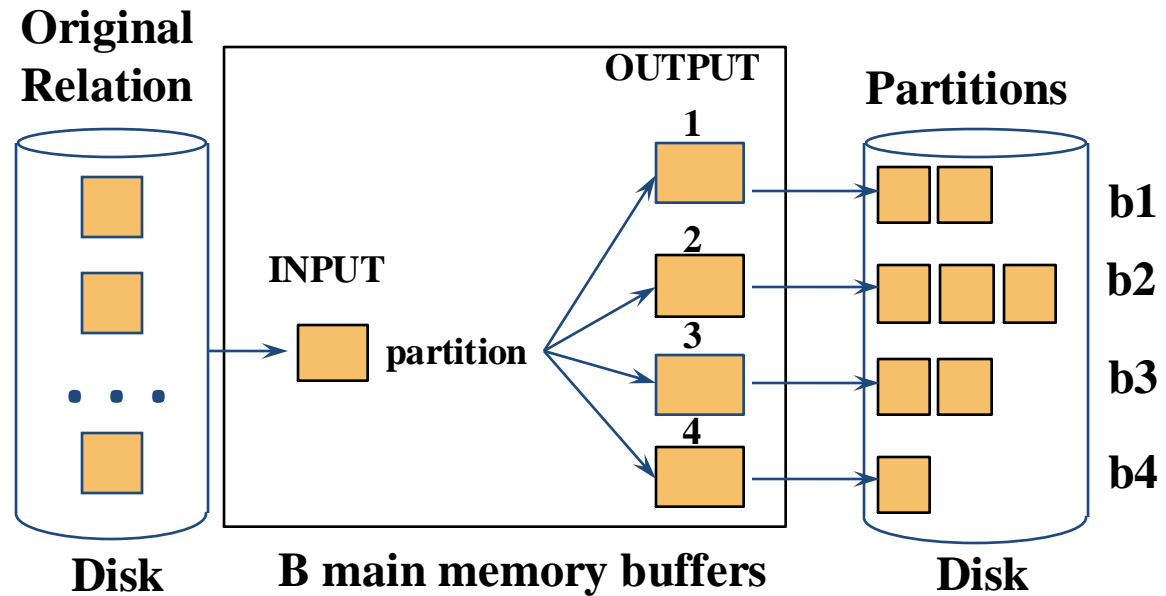
$b1: h \in [1,25]$

$b2: h \in [26,50]$

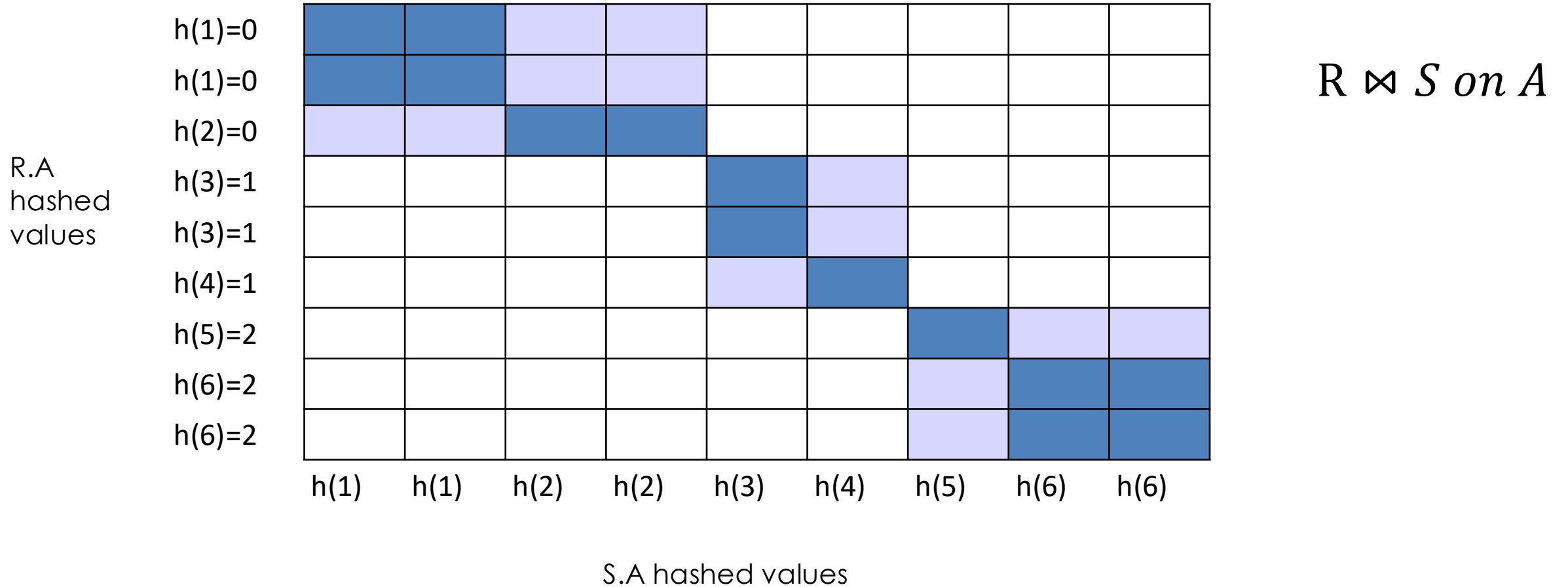
$b3: h \in [51,75]$

$b4: h \in [76,100]$

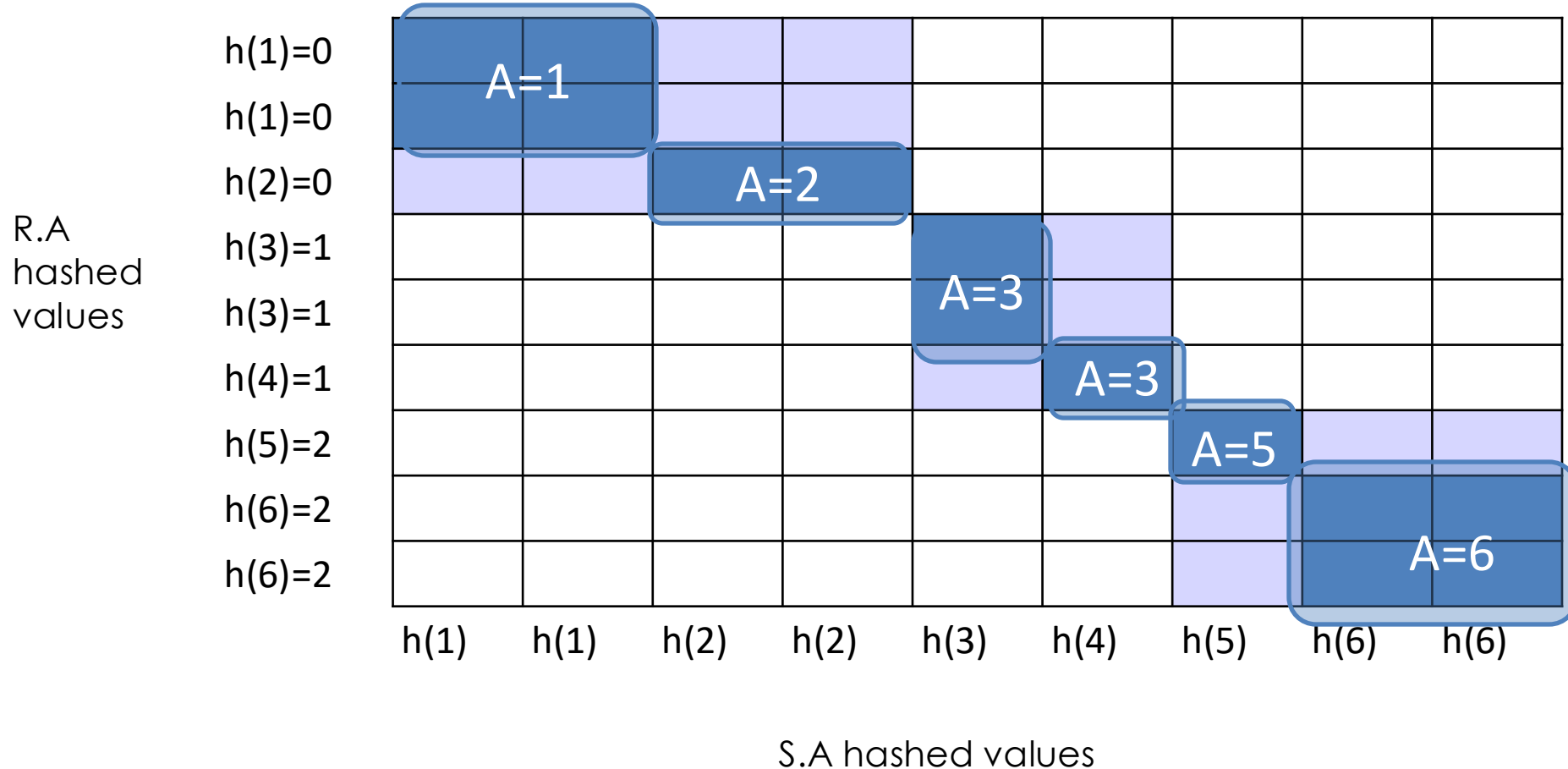
If $|F| \leq |M|$, in second phase build in-memory hash table on F partitions, and stream M partitions through memory



Hash Join Phase 2: Matching



Hash Join Phase 2: Matching

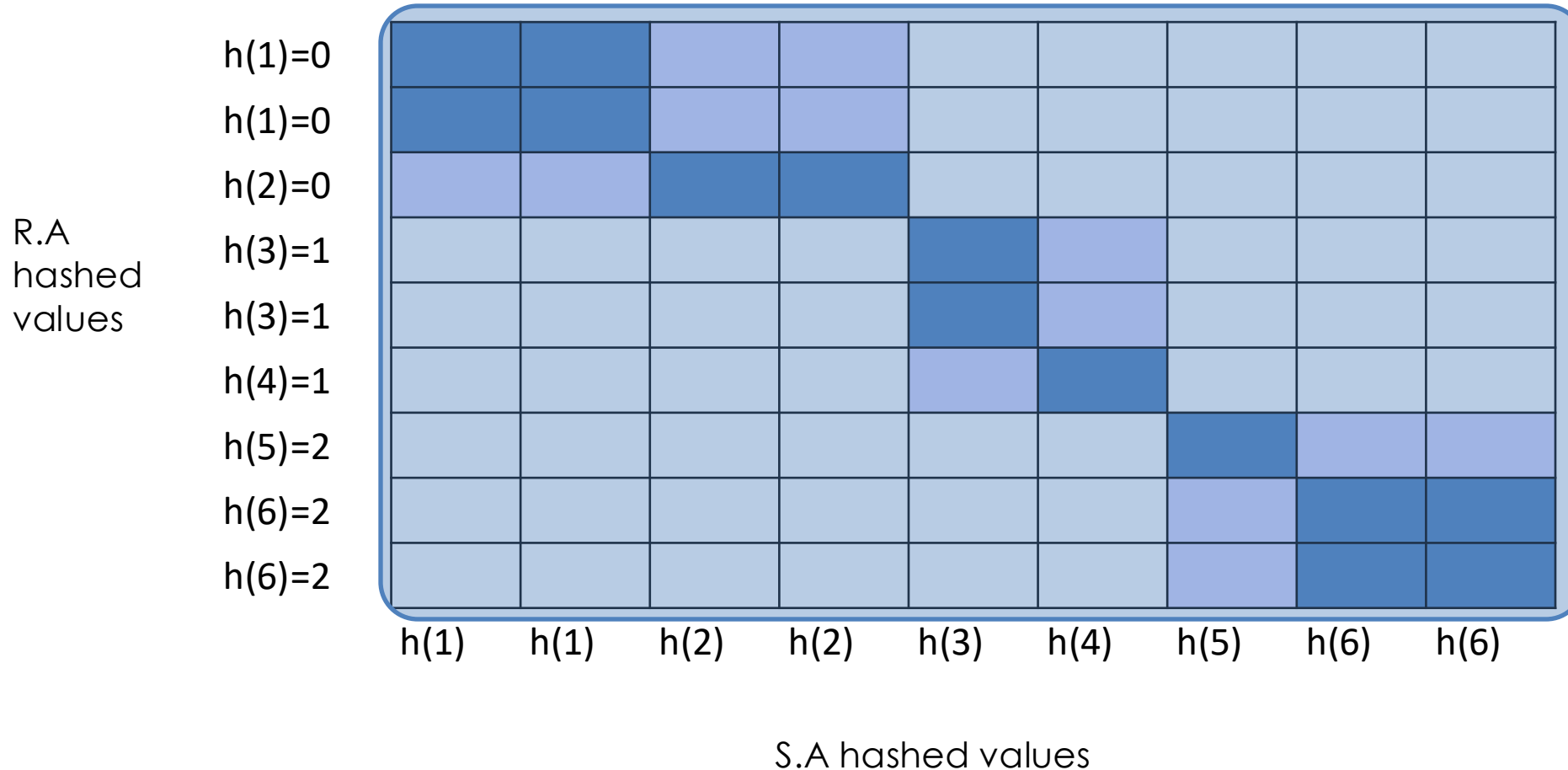


$$R \bowtie S \text{ on } A$$

To perform the join, we ideally just need to explore the dark blue regions

= the tuples with same values of the join key A

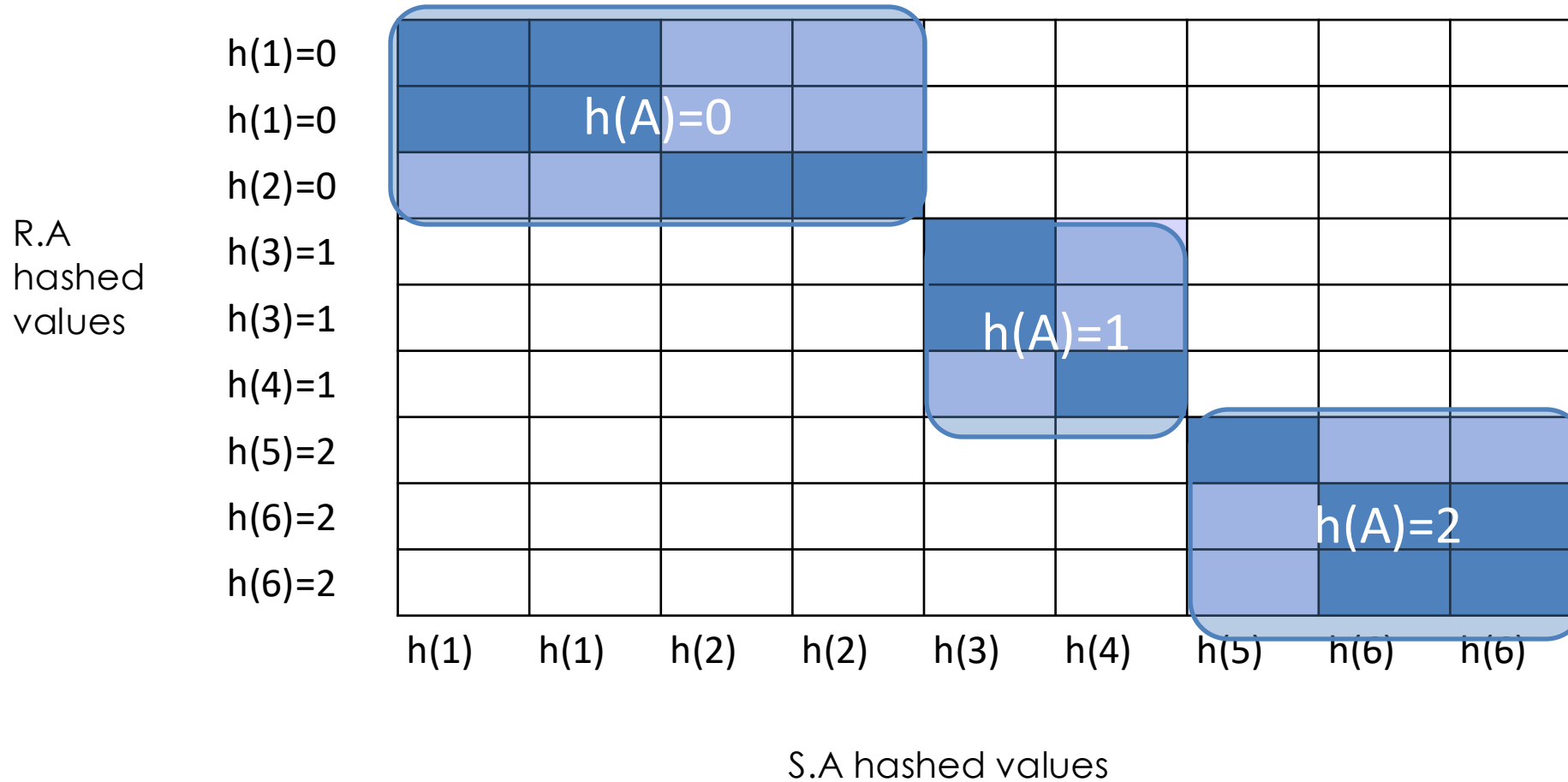
Hash Join Phase 2: Matching



$R \bowtie S \text{ on } A$

With a join algorithm like BNLJ that doesn't take advantage of equijoin structure, we'd have to explore this whole grid!

Hash Join Phase 2: Matching



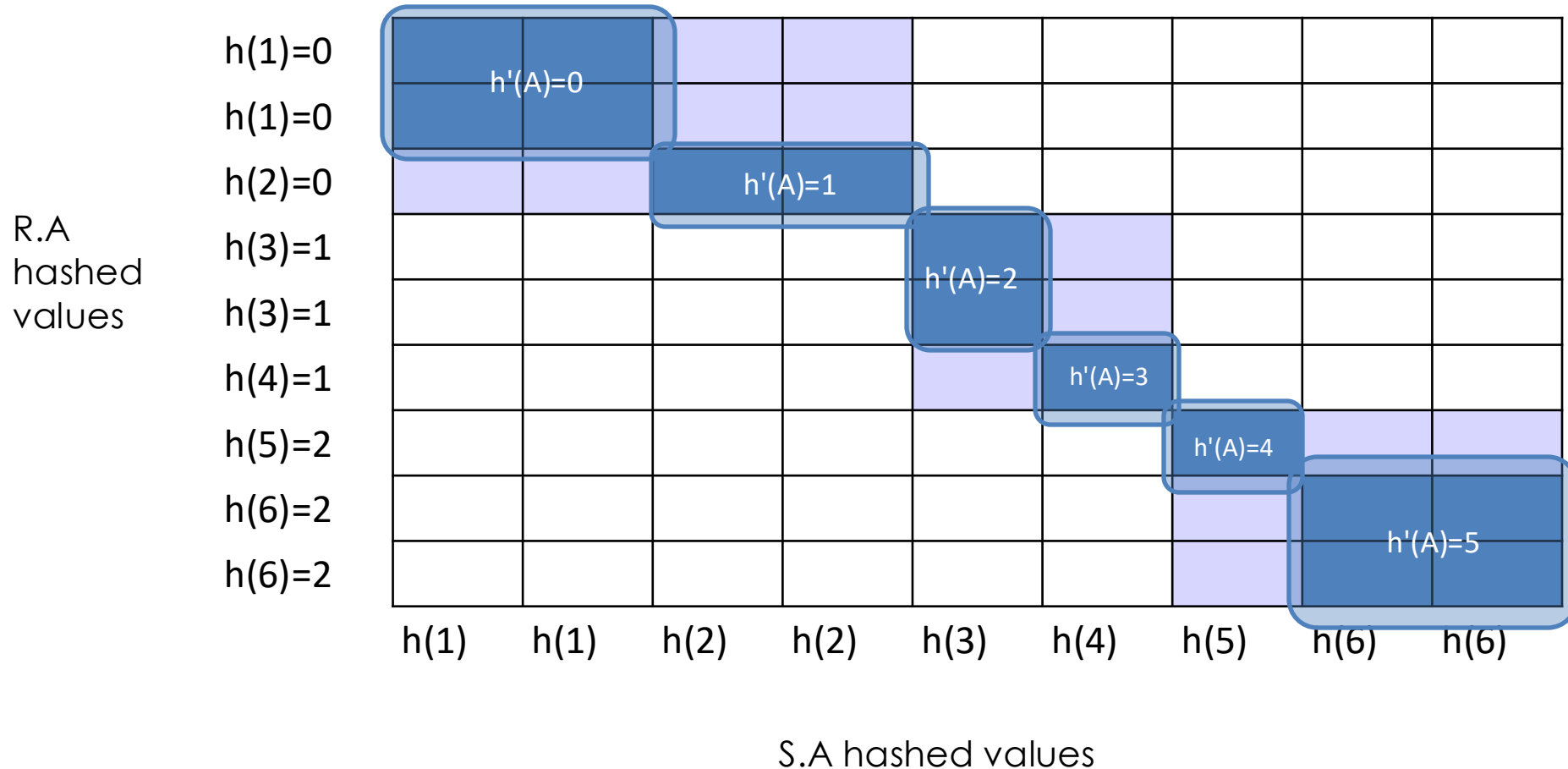
$$R \bowtie S \text{ on } A$$

With HJ, we only explore the blue regions

= the tuples with same values of $h(A)$!

We can apply BNLJ to each of these regions

Hash Join Phase 2: Matching



$R \bowtie S \text{ on } A$

An alternative to applying BNLJ:

We could also hash again, and keep doing passes in memory to reduce further!

Summary

Sort merge join

- Relies on the sorted order of join attributes
- Produces sorted output

Hash join

- Uses little memory
- Great when one relations is much smaller than the other
- Has problems with data skew

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General joins and aggregates

Readings: Chapters 14.4.5-14.7

General Join Conditions

Equalities over several attributes

(e.g., *R.sid=S.sid AND R.rname=S.sname*):

- For Index NL, build index on *<sid, sname>* (if S is inner); or use existing indexes on *sid* or *sname*
- For Sort-Merge and Hash Join, sort/partition on combination of the two join columns

Inequality conditions (e.g., *R.rname < S.sname*):

- For Index NL, need (clustered!) B+ tree index
 - Range probes on inner; # matches likely to be much higher than for equality joins
- Hash Join, Sort Merge Join not applicable!
- Block NL quite likely to be the best join method here

Set Operations

Intersection and ***cross-product*** special cases of join

Union (Distinct) and **Except** similar; we'll do **union**:

Sorting based approach to union:

- Sort both relations (on combination of all attributes)
- Scan sorted relations and merge them
- *Alternative*: Merge runs from Pass 0 for *both* relations

Hash based approach to union:

- Partition R and S using hash function h
- For each S-partition, build in-memory hash table (using h_2), scan corresponding R-partition and add tuples to table while discarding duplicates

Aggregate Operations (AVG, MIN, etc.)

Without grouping:

- In general, requires *scanning* the relation
- Given *index* whose search key *includes all attributes in the SELECT or WHERE* clauses, can do index-only scan

Example: SELECT avg(salary) FROM EMPLOYEES WHERE age>35

can use an index on **<age, salary>** without going to the base data

Aggregate Operations (AVG, MIN, etc.)

With grouping:

- (a) **sort** on group-by attributes
- (b) scan relation and compute aggregate for each group
- Note: we can improve upon this by **combining** sorting and aggregation
- Similar approach based on **hashing** on group-by attributes
- Given tree **index** whose search key **includes all attributes in SELECT, WHERE and GROUP BY** clauses, we can do index-only scan
- If **group-by attributes form prefix of the search key**, we can retrieve data entries/tuples in group-by order

Impact of Buffering

If several operations are executing concurrently, estimating the number of available buffer pages is guesswork

Repeated access patterns interact with buffer replacement policy

- e.g., Inner relation is scanned repeatedly in Simple Nested Loop Join. With enough buffer pages to hold inner, replacement policy does not matter. Otherwise, MRU is best, LRU is worst (*sequential flooding*)
- Does replacement policy matter for Block Nested Loops?
- What about Index Nested Loops?

Summary

A virtue of relational DBMSs: **queries are composed of a few basic operators**

- Implementation of operators can be **carefully tuned**
- Important to do this!

Many alternative implementations for each operator

- No universally superior technique for most operators

Must consider alternatives for each operation in a query and choose best one based on system statistics...

- Part of the broader task of optimizing a query composed of several operators