Learning Multi-dimensional Indexes

Vikram Nathan*, Jialin Ding*, Mohammad Alizadeh, Tim Kraska





- Why ML?
 - Systems rely on heuristics and hand-tuning
 - Systems don't adapt to specific data/workload

- Why ML?
 - Systems rely on heuristics and hand-tuning
 - Systems don't adapt to specific data/workload
- Examples
 - Query optimization
 - $\circ \quad \text{Job scheduling} \\$
 - \circ Indexing
 - Sorting

- Why ML?
 - Systems rely on heuristics and hand-tuning
 - Systems don't adapt to specific data/workload
- Examples
 - Query optimization
 - Job scheduling
 - Indexing
 - Sorting

Artificial Intelligence / Machine Learning

Google just gave control over data center cooling to an Al

In a first, Google is trusting a self-taught algorithm to manage part of its infrastructure.

by Will Knight

Aug 17, 2018

- Why ML?
 - Systems rely on heuristics and hand-tuning
 - Systems don't adapt to specific data/workload
- Examples
 - Query optimization
 - Job scheduling
 - Indexing
 - Sorting
- Differences with "mainstream" ML:
 - Objectives beyond accuracy (e.g., latency, space usage, cost)
 - Want 10X, not 10%

Artificial Intelligence / Machine Learning

Google just gave control over data center cooling to an Al

In a first, Google is trusting a self-taught algorithm to manage part of its infrastructure.

by Will Knight

Aug 17, 2018

- Why ML?
 - Systems rely on heuristics and hand-tuning
 - Systems don't adapt to specific data/workload
- Examples
 - Query optimization
 - Job scheduling
 - Indexing
 - Sorting
- Differences with "mainstream" ML:
 - Objectives beyond accuracy (e.g., latency, space usage, cost)
 - Want 10X, not 10%
 - Implication: favor creative uses of simple models

Artificial Intelligence / Machine Learning

Google just gave control over data center cooling to an Al

In a first, Google is trusting a self-taught algorithm to manage part of its infrastructure.

by Will Knight

Aug 17, 2018

Outline

- 1. Completed work: Flood (SIGMOD 2020)
- 2. Future work: column correlations, query skew, categorical attributes







<u>Order</u> ID	ltem ID	Ship Date	Receipt Date	Price	Quantity	Discount	Тах
1	42	9/14/19	9/16/19	2	1	0	5%
2	137	9/18/19	9/25/19	5	1	0	6.5%
3	314	10/3/19	10/6/19	14	2	0	5.5%
4	272	9/30/19	10/15/19	52	1	0.1	8%
5	162	10/2/19	10/4/19	13	1	0	6.5%
6	602	10/5/19	10/10/19	7	5	0.5	8.5%
7	141	10/4/19	10/9/19	150	1	0.1	7%
8	173	10/8/19	10/12/19	20	2	0	8%

<u>Order</u> ID	ltem ID	Ship Date	Receipt Date	Price	Quantity	Discount	Тах
1	42	9/14/19	9/16/19	2	1	0	5%
2	137	9/18/19	9/25/19	5	1	0	6.5%
3	314	10/3/19	10/6/19	14	2	0	5.5%
4	272	9/30/19	10/15/19	52	1	0.1	8%
5	162	10/2/19	10/4/19	13	1	0	6.5%
6	602	10/5/19	10/10/19	7	5	0.5	8.5%
7	141	10/4/19	10/9/19	150	1	0.1	7%
8	173	10/8/19	10/12/19	20	2	0	8%

<u>Query</u>

SELECT COUNT(*) FROM table WHERE Price >= 10 AND Price < 100

<u>Order</u>	Item	Ship	Receipt	Price	Quantity	Discount	Тах	Query
<u>ID</u>	ID	Date	Date					SELECT COUNT(*)
1	42	9/14/19	9/16/19	2	1	0	5%	FROM table WHERE Price >= 10
2	137	9/18/19	9/25/19	5	1	0	6.5%	AND Price < 100
3	314	10/3/19	10/6/19	14	2	0	5.5%	
4	272	9/30/19	10/15/19	52	1	0.1	8%	
5	162	10/2/19	10/4/19	13	1	0	6.5%	
6	602	10/5/19	10/10/19	7	5	0.5	8.5%	
7	141	10/4/19	10/9/19	150	1	0.1	7%	
8	173	10/8/19	10/12/19	20	2	0	8%	

<u>Order</u> ID	ltem ID	Ship Date	Receipt Date	Price	Quantity	Discount	Тах
1	42	9/14/19	9/16/19	2	1	0	5%
2	137	9/18/19	9/25/19	5	1	0	6.5%
3	314	10/3/19	10/6/19	14	2	0	5.5%
4	272	9/30/19	10/15/19	52	1	0.1	8%
5	162	10/2/19	10/4/19	13	1	0	6.5%
6	602	10/5/19	10/10/19	7	5	0.5	8.5%
7	141	10/4/19	10/9/19	150	1	0.1	7%
8	173	10/8/19	10/12/19	20	2	0	8%

<u>Query</u>

SELECT COUNT(*) FROM table WHERE Price >= 10 AND Price < 100

<u>Order</u> ID	ltem ID	Ship Date	Receipt Date	Price	Quantity	Discount	Тах
1	42	9/14/19	9/16/19	2	1	0	5%
2	137	9/18/19	9/25/19	5	1	0	6.5%
3	314	10/3/19	10/6/19	14	2	0	5.5%
4	272	9/30/19	10/15/19	52	1	0.1	8%
5	162	10/2/19	10/4/19	13	1	0	6.5%
6	602	10/5/19	10/10/19	7	5	0.5	8.5%
7	141	10/4/19	10/9/19	150	1	0.1	7%
8	173	10/8/19	10/12/19	20	2	0	8%

<u>Query</u>

SELECT COUNT(*) FROM table WHERE Price >= 10 AND Price < 100

Scan overhead: ratio of records scanned to number of filtered results

<u>Order</u> ID	ltem ID	Ship Date	Receipt Date	Price	Quantity	Discount	Тах
1	42	9/14/19	9/16/19	2	1	0	5%
2	137	9/18/19	9/25/19	5	1	0	6.5%
3	314	10/3/19	10/6/19	14	2	0	5.5%
4	272	9/30/19	10/15/19	52	1	0.1	8%
5	162	10/2/19	10/4/19	13	1	0	6.5%
6	602	10/5/19	10/10/19	7	5	0.5	8.5%
7	141	10/4/19	10/9/19	150	1	0.1	7%
8	173	10/8/19	10/12/19	20	2	0	8%

QueryScan OverheadSELECT COUNT(*)2FROM tableWHERE Price >= 10AND Price < 100</td>

Scan overhead: ratio of records scanned to number of filtered results

<u>Order</u> ID	ltem ID	Ship Date	Receipt Date	Price	Quantity	Discount	Тах
1	42	9/14/19	9/16/19	2	1	0	5%
2	137	9/18/19	9/25/19	5	1	0	6.5%
3	314	10/3/19	10/6/19	14	2	0	5.5%
4	272	9/30/19	10/15/19	52	1	0.1	8%
5	162	10/2/19	10/4/19	13	1	0	6.5%
6	602	10/5/19	10/10/19	7	5	0.5	8.5%
7	141	10/4/19	10/9/19	150	1	0.1	7%
8	173	10/8/19	10/12/19	20	2	0	8%

QueryScan OverheadSELECT COUNT(*)2FROM tableWHERE Price >= 10AND Price < 100</td>

Scan overhead: ratio of records scanned to number of filtered results

Lower scan overhead generally leads to lower query time

Order ID	ltem ID	Ship Date	Receipt Date	<u>Price</u>	Quantity	Discount	Тах
1	42	9/14/19	9/16/19	2	1	0	5%
2	137	9/18/19	9/25/19	5	1	0	6.5%
6	602	10/5/19	10/10/19	7	5	0.5	8.5%
5	162	10/2/19	10/4/19	13	1	0	6.5%
3	314	10/3/19	10/6/19	14	2	0	5.5%
8	173	10/8/19	10/12/19	20	2	0	8%
4	272	9/30/19	10/15/19	52	1	0.1	8%
7	141	10/4/19	10/9/19	150	1	0.1	7%

<u>Query</u>

SELECT COUNT(*) FROM table WHERE Price >= 10 AND Price < 100

Order ID	ltem ID	Ship Date	Receipt Date	<u>Price</u>	Quantity	Discount	Тах
1	42	9/14/19	9/16/19	2	1	0	5%
2	137	9/18/19	9/25/19	5	1	0	6.5%
6	602	10/5/19	10/10/19	7	5	0.5	8.5%
5	162	10/2/19	10/4/19	13	1	0	6.5%
3	314	10/3/19	10/6/19	14	2	0	5.5%
8	173	10/8/19	10/12/19	20	2	0	8%
4	272	9/30/19	10/15/19	52	1	0.1	8%
7	141	10/4/19	10/9/19	150	1	0.1	7%

QueryScan OverheadSELECT COUNT(*)1FROM tableWHERE Price >= 10AND Price < 100</td>

Order ID	ltem ID	Ship Date	Receipt Date	<u>Price</u>	Quantity	Discount	Тах
1	42	9/14/19	9/16/19	2	1	0	5%
2	137	9/18/19	9/25/19	5	1	0	6.5%
6	602	10/5/19	10/10/19	7	5	0.5	8.5%
5	162	10/2/19	10/4/19	13	1	0	6.5%
3	314	10/3/19	10/6/19	14	2	0	5.5%
8	173	10/8/19	10/12/19	20	2	0	8%
4	272	9/30/19	10/15/19	52	1	0.1	8%
7	141	10/4/19	10/9/19	150	1	0.1	7%

Query	<u>Scan Overhead</u>
SELECT COUNT(*) FROM table WHERE Price >= 10 AND Price < 1	
SELECT COUNT(*) FROM table	

WHERE Price >= 10

AND Price < 100 AND Quantity = 1

Order ID	ltem ID	Ship Date	Receipt Date	<u>Price</u>	Quantity	Discount	Тах
1	42	9/14/19	9/16/19	2	1	0	5%
2	137	9/18/19	9/25/19	5	1	0	6.5%
6	602	10/5/19	10/10/19	7	5	0.5	8.5%
5	162	10/2/19	10/4/19	13	1	0	6.5%
3	314	10/3/19	10/6/19	14	2	0	5.5%
8	173	10/8/19	10/12/19	20	2	0	8%
4	272	9/30/19	10/15/19	52	1	0.1	8%
7	141	10/4/19	10/9/19	150	1	0.1	7%

QueryScan OverheadSELECT COUNT(*)1FROM tableWHERE Price >= 10AND Price < 100</td>

SELECT COUNT(*) FROM table WHERE Price >= 10 AND Price < 100 AND Quantity = 1 2

Order ID	ltem ID	Ship Date	Receipt Date	<u>Price</u>	Quantity	Discount	Тах
1	42	9/14/19	9/16/19	2	1	0	5%
2	137	9/18/19	9/25/19	5	1	0	6.5%
6	602	10/5/19	10/10/19	7	5	0.5	8.5%
5	162	10/2/19	10/4/19	13	1	0	6.5%
3	314	10/3/19	10/6/19	14	2	0	5.5%
8	173	10/8/19	10/12/19	20	2	0	8%
4	272	9/30/19	10/15/19	52	1	0.1	8%
7	141	10/4/19	10/9/19	150	1	0.1	7%

Query	<u>Scan Overhead</u>
SELECT COUNT(*) FROM table WHERE Price >= 10 AND Price < 10	1
	-

SELECT COUNT(*) FROM table WHERE Price >= 10 AND Price < 100 AND Quantity = 1

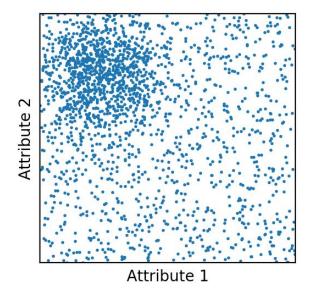
SELECT COUNT(*) FROM table WHERE Quantity > 2 2

Order ID	ltem ID	Ship Date	Receipt Date	<u>Price</u>	Quantity	Discount	Тах
1	42	9/14/19	9/16/19	2	1	0	5%
2	137	9/18/19	9/25/19	5	1	0	6.5%
6	602	10/5/19	10/10/19	7	5	0.5	8.5%
5	162	10/2/19	10/4/19	13	1	0	6.5%
3	314	10/3/19	10/6/19	14	2	0	5.5%
8	173	10/8/19	10/12/19	20	2	0	8%
4	272	9/30/19	10/15/19	52	1	0.1	8%
7	141	10/4/19	10/9/19	150	1	0.1	7%

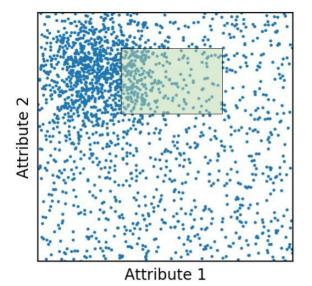
Query	<u>Scan Overhead</u>
SELECT COUNT(*) FROM table WHERE Price >= 10 AND Price < 10	1
SELECT COUNT(*) FROM table WHERE Price >= 10 AND Price < 10 AND Quantity =	
SELECT COUNT(*) FROM table	8

WHERE Quantity > 2

Multi-dimensional indexes



Multi-dimensional indexes



<u>Query</u>

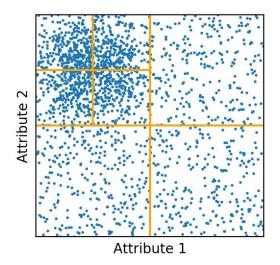
SELECT COUNT(*) FROM table

WHERE Attribute 1 >= A

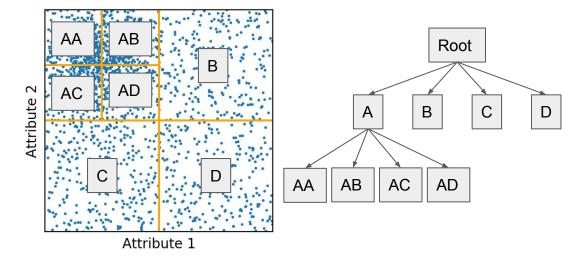
AND Attribute 1 <= B

AND Attribute 2 >= C

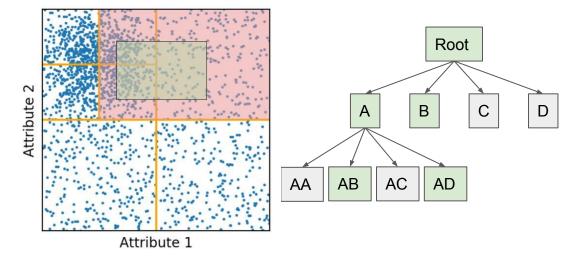
AND Attribute 2 <= D



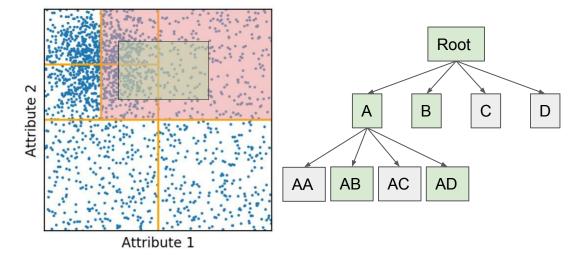
• Quadtree (hyper-octree in higher dimensions)



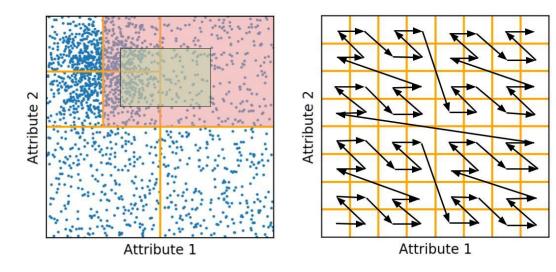
• Quadtree (hyper-octree in higher dimensions)



• Quadtree (hyper-octree in higher dimensions)

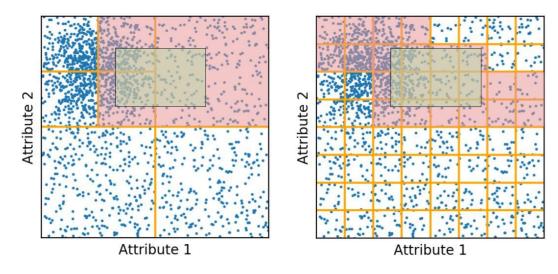


- Quadtree (hyper-octree in higher dimensions)
- Other tree-based indexes: R-tree, k-d tree
- Geospatial databases



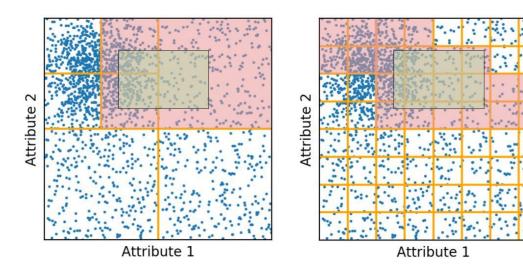
Z-order

- Quadtree (hyper-octree in higher dimensions)
- Other tree-based indexes: R-tree, k-d tree
- Geospatial databases



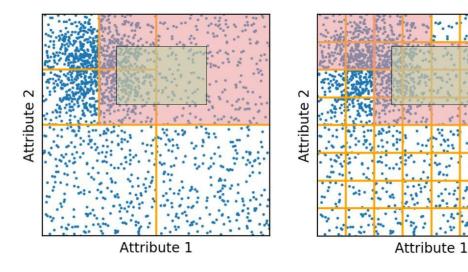
Z-order

- Quadtree (hyper-octree in higher dimensions)
- Other tree-based indexes: R-tree, k-d tree
- Geospatial databases



- Quadtree (hyper-octree in higher dimensions)
- Other tree-based indexes: R-tree, k-d tree
- Geospatial databases

- Z-order
- Other sort-order-based indexes: UB-tree
- Amazon Redshift



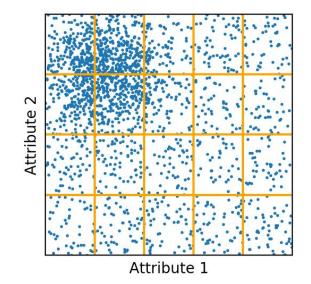
- Drawbacks
 - Difficult to create and maintain, requires DBA
 - No index dominates all others
 - Does not allow fined-grained customization

- Quadtree (hyper-octree in higher dimensions)
- Other tree-based indexes: R-tree, k-d tree
- Geospatial databases

- Z-order
- Other sort-order-based indexes: UB-tree
- Amazon Redshift

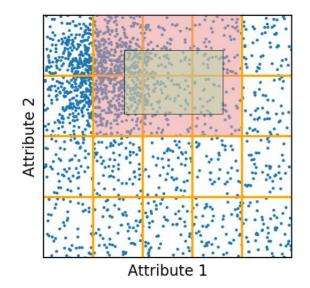
Our new index: Flood

- Multi-dimensional in-memory read-optimized index
- Grid-based layout



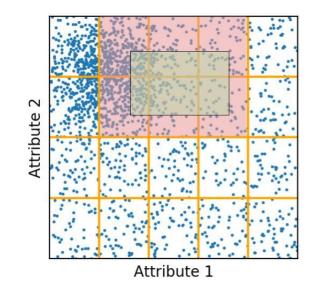
Our new index: Flood

- Multi-dimensional in-memory read-optimized index
- Grid-based layout



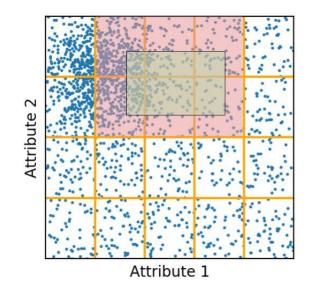
Our new index: Flood

- Multi-dimensional in-memory read-optimized index
- Grid-based layout
 - Low index time (vs. tree-based index)
 - Has good number of tunable parameters



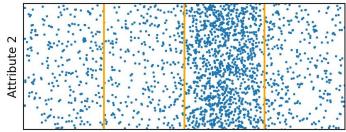
Our new index: Flood

- Multi-dimensional in-memory read-optimized index
- Grid-based layout
 - Low index time (vs. tree-based index)
 - Has good number of tunable parameters
- Key idea: learning-based approach to jointly optimize the index structure and layout
 - Learn from data
 - $\circ \quad \text{Learn from queries} \\$



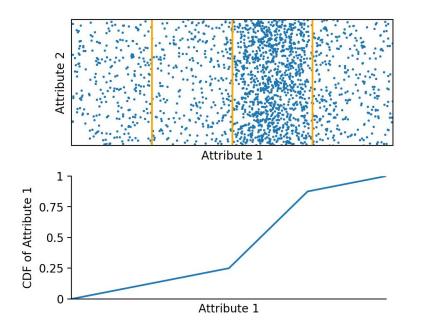
• Goal: uniform number of points per cell

• Goal: uniform number of points per cell

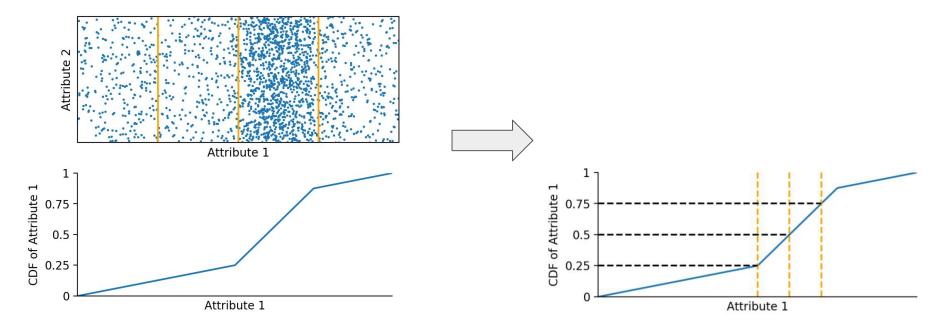


Attribute 1

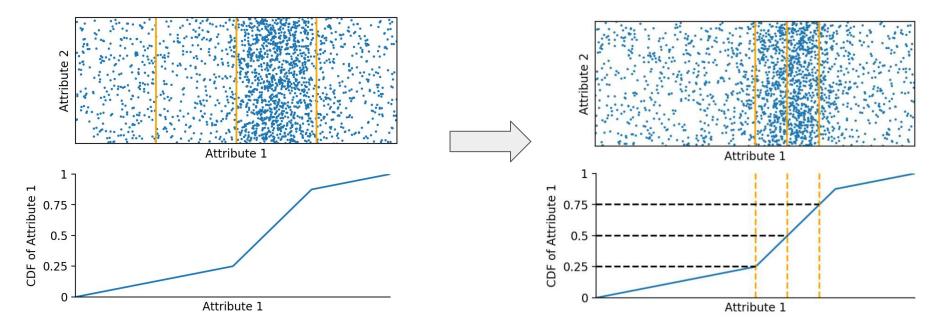
- Goal: uniform number of points per cell
- Key idea: model the CDF of each dimension



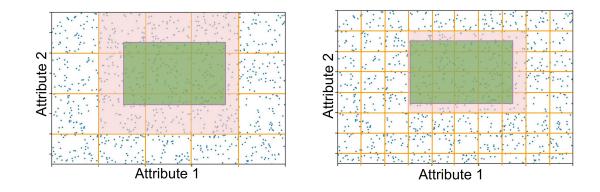
- Goal: uniform number of points per cell
- Key idea: model the CDF of each dimension



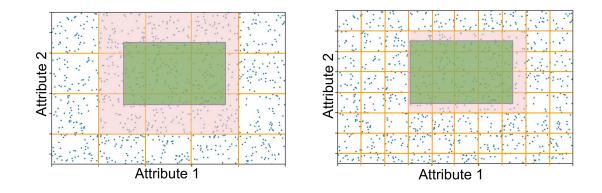
- Goal: uniform number of points per cell
- Key idea: model the CDF of each dimension



 Goal: find optimal number of partitions in each dimension

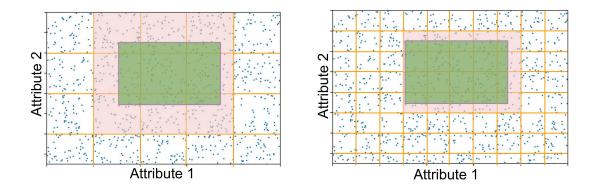


 Goal: find optimal number of partitions in each dimension



- Pro: Lower scan overhead
- Con: More cells

 Goal: find optimal number of partitions in each dimension

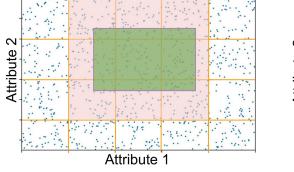


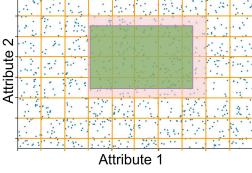
- Pro: Fewer cells
- Con: Higher scan overhead

- Pro: Lower scan overhead
- Con: More cells

- Goal: find optimal number of partitions in each dimension
- Key idea: use cost model to predict query time

$$Time(D,q,L) = w_c N_c + w_s N_s$$
cells # scanned points



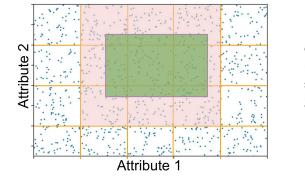


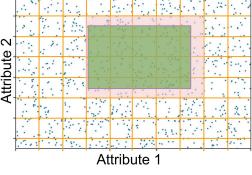
- Pro: Fewer cells
- Con: Higher scan overhead

- Pro: Lower scan overhead
- Con: More cells

- Goal: find optimal number of partitions in each dimension
- Key idea: use cost model to predict query time

$$Time(D,q,L) = w_c N_c + w_s N_s$$
cells # scanned points

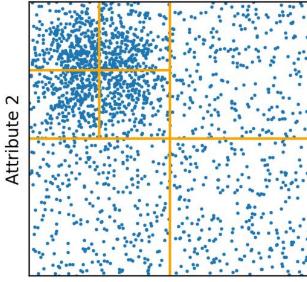




- Solve for layout with lowest average query time using gradient descent
- Pro: Fewer cells
- Con: Higher scan overhead

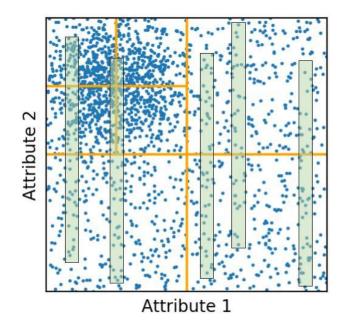
- Pro: Lower scan overhead
- Con: More cells

Quadtree

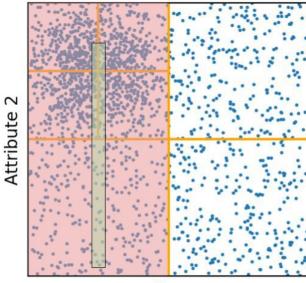


Attribute 1

Quadtree



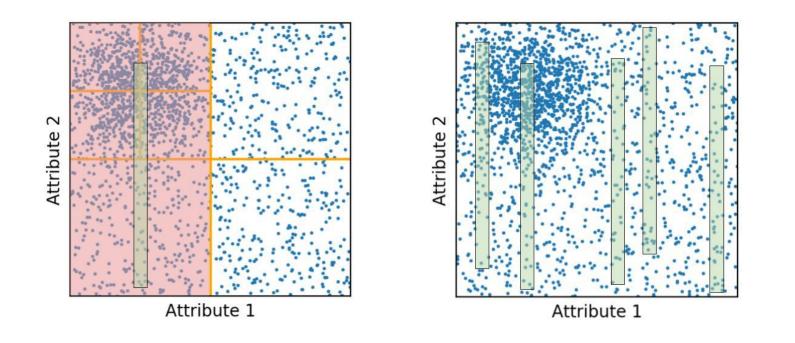
Quadtree



Attribute 1

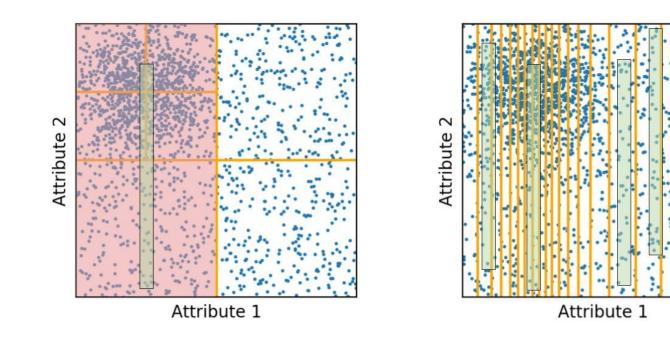
Quadtree

Flood



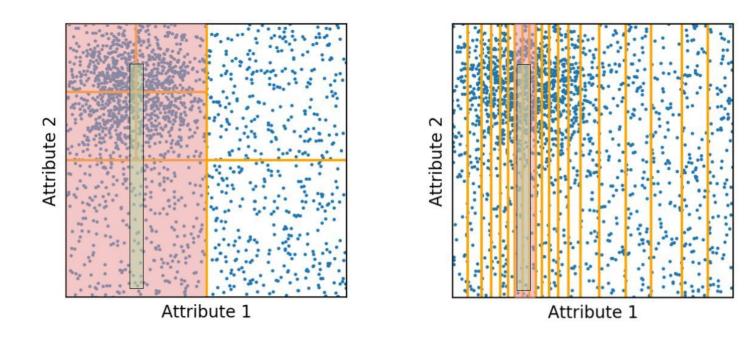
Quadtree

Flood



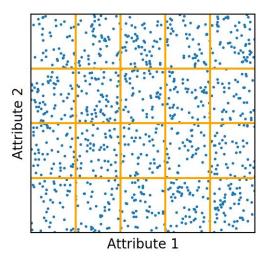
Quadtree

Flood



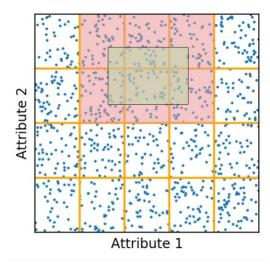
"Naive" grid

- Grid over d dimensions
- Cells are ordered
- Within each cell, points are unsorted



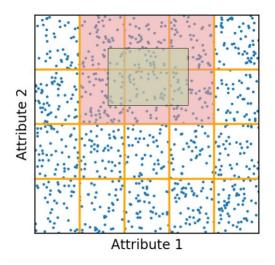
"Naive" grid

- Grid over d dimensions
- Cells are ordered
- Within each cell, points are unsorted



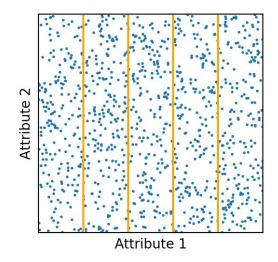
"Naive" grid

- Grid over d dimensions
- Cells are ordered
- Within each cell, points are unsorted



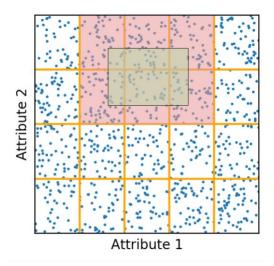
Flood's grid

- Grid over d-1 dimensions
- Cells are ordered
- Within each cell, points are sorted by d-th dimension



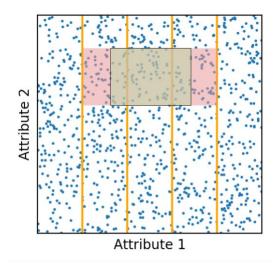
"Naive" grid

- Grid over d dimensions
- Cells are ordered
- Within each cell, points are unsorted



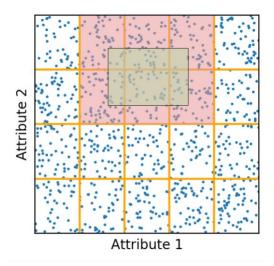
Flood's grid

- Grid over d-1 dimensions
- Cells are ordered
- Within each cell, points are sorted by d-th dimension



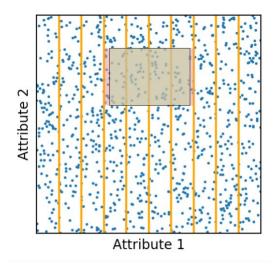
"Naive" grid

- Grid over d dimensions
- Cells are ordered
- Within each cell, points are unsorted

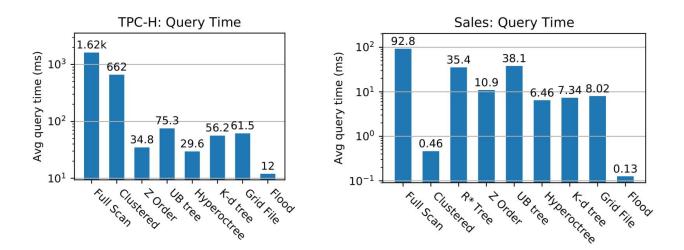


Flood's grid

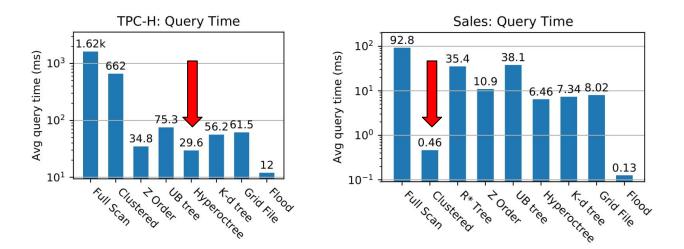
- Grid over d-1 dimensions
- Cells are ordered
- Within each cell, points are sorted by d-th dimension



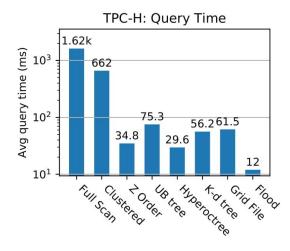
- How does Flood compare to other indexes?
 - Faster than every other index



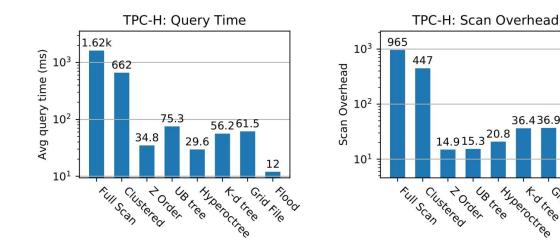
- How does Flood compare to other indexes?
 - Faster than every other index



- How does Flood compare to other indexes?
 - Faster than every other index
- Where does Flood's advantage come from?
 - Low scan overhead



- How does Flood compare to other indexes? •
 - Faster than every other index Ο
- Where does Flood's advantage come from? •
 - Low scan overhead Ο



36.436.9

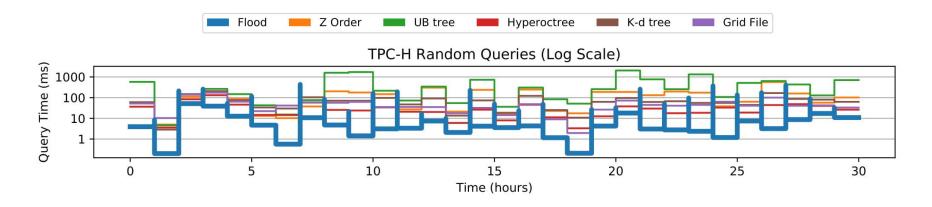
Hyperoctree

tatree

5.9

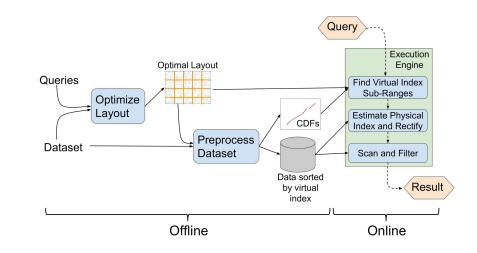
Grid File £1000

- How does Flood compare to other indexes?
 - Faster than every other index
- Where does Flood's advantage come from?
 - Low scan overhead
- What if the query workload changes?
 - Flood can adapt



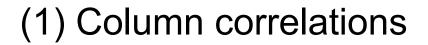
Summary of Flood

- Multi-dimensional in-memory read-optimized index
- Automatically learned based on data distribution and query workload
- Outperforms all other indexes by achieving lower scan overhead

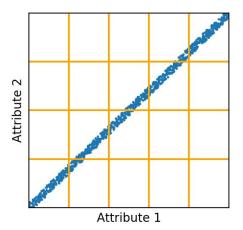


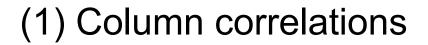
Outline

- 1. Completed work: Flood (SIGMOD 2020)
- 2. Future work: column correlations, query skew, categorical attributes

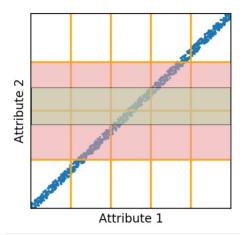


Monotonic correlations



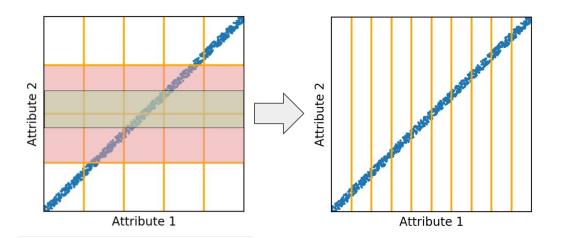


Monotonic correlations



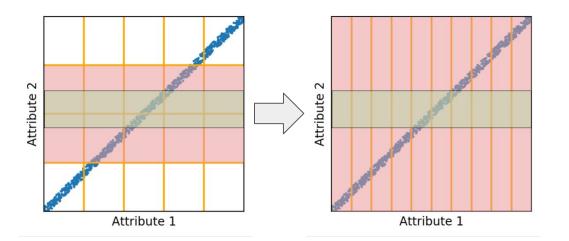
Monotonic correlations

• Possible solution: function-based mapping



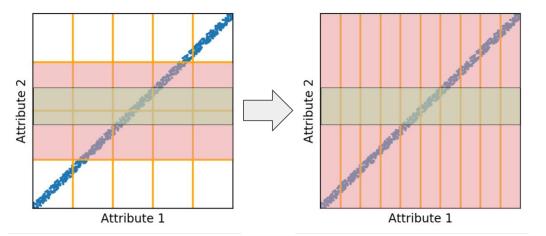
Monotonic correlations

• Possible solution: function-based mapping



Monotonic correlations

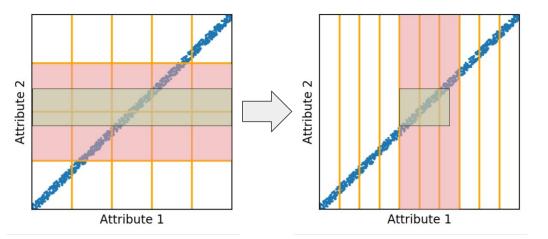
• Possible solution: function-based mapping



[A_min, A_max] = Fn([B_min, B_max]) + error

Monotonic correlations

• Possible solution: function-based mapping

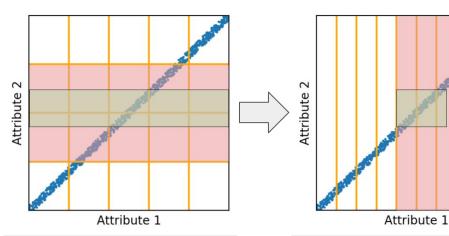


[A_min, A_max] = Fn([B_min, B_max]) + error

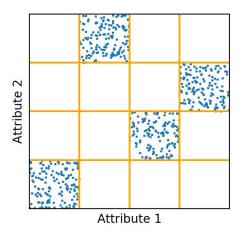
(1) Column correlations

Monotonic correlations

• Possible solution: function-based mapping



[A_min, A_max] = Fn([B_min, B_max]) + error

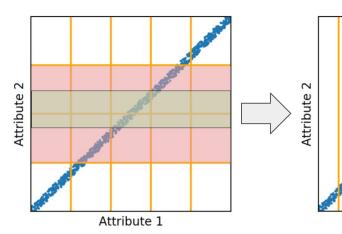


Hotspots

(1) Column correlations

Monotonic correlations

Possible solution: function-based mapping

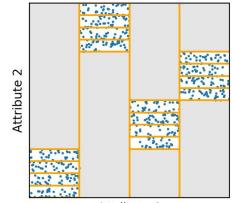


[A_min, A_max] = Fn([B_min, B_max]) + error

Attribute 1

Hotspots

Possible solution: "non-uniform grid"





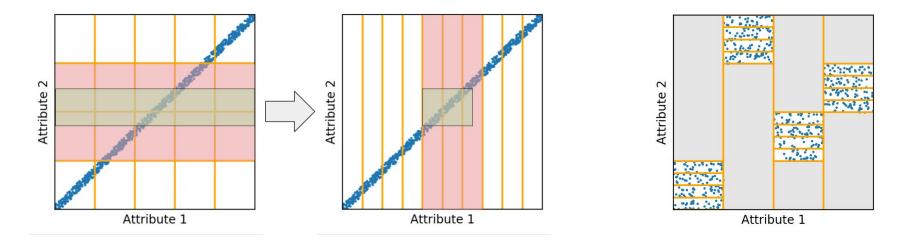
(1) Column correlations

Monotonic correlations

• Possible solution: function-based mapping

<u>Hotspots</u>

Possible solution: "non-uniform grid"

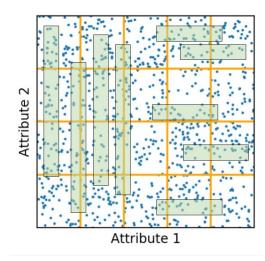


[A_min, A_max] = Fn([B_min, B_max]) + error

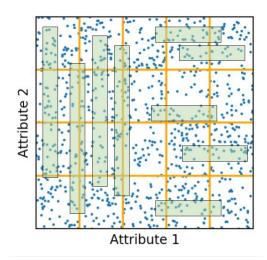
Challenge: combinatorial explosion of possible layouts

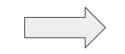
- Queries "look different" in different regions
 - Selectivity
 - Frequency

- Queries "look different" in different regions
 - Selectivity
 - \circ Frequency

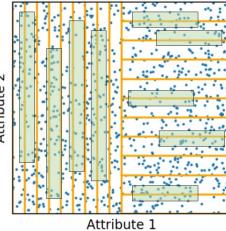


- Queries "look different" in different regions
 - Selectivity
 - Frequency



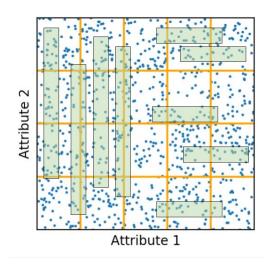


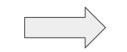
Attribute 2



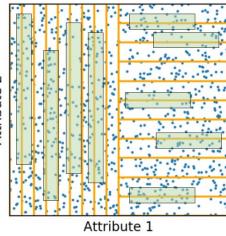
- Queries "look different" in different regions
 - Selectivity
 - Frequency

- Possible solution: "Flood tree"
 - Lightweight decision tree
 - Each leaf node is an instance of Flood









- Opportunity 1: No semantic sort order
 - Order based on co-access frequency

- Opportunity 1: No semantic sort order
 - Order based on co-access frequency
- Opportunity 2: Column correlations
 - Direct mapping

rid	<u>State</u>	City	
0	IL	Springfield	
1	MA	Salem	
2	MA	Springfield	
3	MA	Salem	
4	МО	Springfield	
5	OR	Salem	

- Opportunity 1: No semantic sort order
 - Order based on co-access frequency
- Opportunity 2: Column correlations
 - Direct mapping

rid	<u>State</u>	City	
0	IL	Springfield	
1	MA	Salem	
2	MA	Springfield	
3	MA	Salem	
4	МО	Springfield	
5	OR	Salem	

	City	rid
ľ	Salem	1
	Salem	3
>	Salem	5
	Springfield	0
	Springfield	2
	Springfield	4

- Opportunity 1: No semantic sort order
 - Order based on co-access frequency
- Opportunity 2: Column correlations
 - Direct mapping

rid	<u>State</u>	City	•••
0	IL	Springfield	
1	MA	Salem	
2	MA	Springfield	
3	MA	Salem	
4	МО	Springfield	
5	OR	Salem	

Secondary index

	-	
	City	rid
	Salem	1
	Salem	3
>	Salem	5
	Springfield	0
	Springfield	2
	Springfield	4

Direct Mapping

City	State
Salem	{MA, OR}
Springfield	{IL, MA, MO}

- Opportunity 1: No semantic sort order
 - Order based on co-access frequency
- Opportunity 2: Column correlations
 - Direct mapping

rid	<u>State</u>	City	
0	IL	Springfield	
1	MA	Salem	
2	MA	Springfield	
3	MA	Salem	
4	МО	Springfield	
5	OR	Salem	

Secondary index

	City	rid
	Salem	1
	Salem	3
>	Salem	5
	Springfield	0
	Springfield	2
	Springfield	4

Direct Mapping

City	State
Salem	{MA, OR}
Springfield	{IL, MA, MO}

- Opportunity 1: No semantic sort order
 - Order based on co-access frequency
- Opportunity 2: Column correlations
 - Direct mapping

rid	<u>State</u>	City	
0	IL	Springfield	
1	MA	Salem	
2	MA	Springfield	
3	MA	Salem	
4	МО	Springfield	
5	OR	Salem	

Secondary index

City	rid
Salem	1
Salem	3
Salem	5
Springfield	0
Springfield	2
Springfield	4

Direct Mapping

City	State
Salem	{MA, OR}
Springfield	{IL, MA, MO}

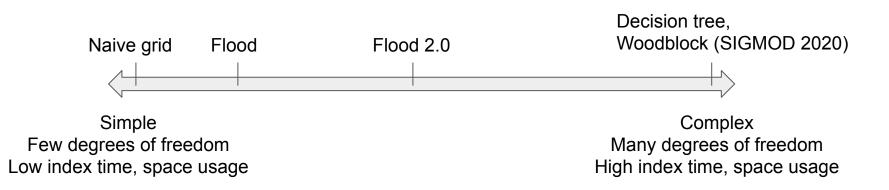
Pro: smaller space Con: higher scan overhead?

Summary of Future Work

- Column correlations
 - Solution: function-based mapping, non-uniform grid
- Query skew
 - Solution: Flood tree
- Categorical attributes
 - Solution: ordering based on co-access frequency, direct mapping

Summary of Future Work

- Column correlations
 - Solution: function-based mapping, non-uniform grid
- Query skew
 - Solution: Flood tree
- Categorical attributes
 - Solution: ordering based on co-access frequency, direct mapping



http://dsg.csail.mit.edu/mlforsystems/